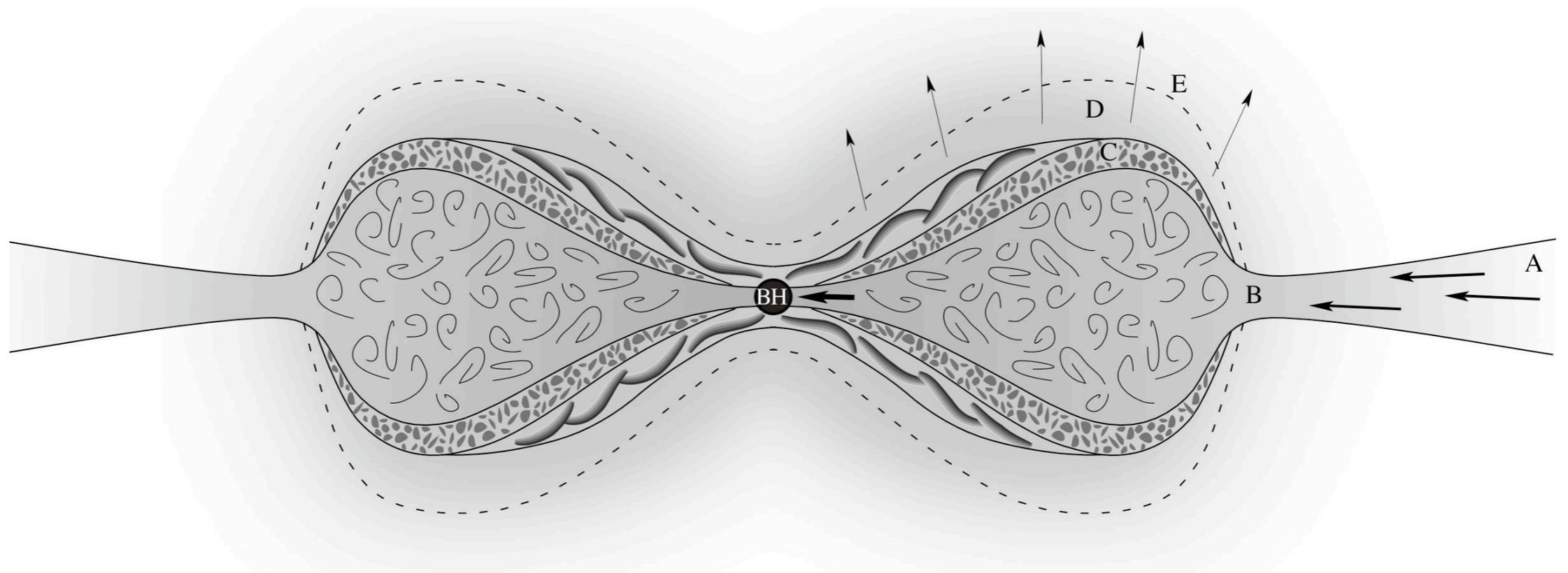
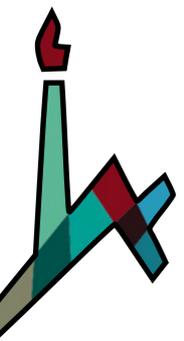


# Super-Eddington **Slim** Accretion disks (and other objects helping us to understand what these accretion disks look like!)



Nir Shaviv  
Hebrew University of Jerusalem

Slim Accretion Disk workshop 2018



# Synopsis

- Super-Eddington objects in nature
- How can it be?
- What do super-Eddington systems look like?
- Implications to Accretion Systems

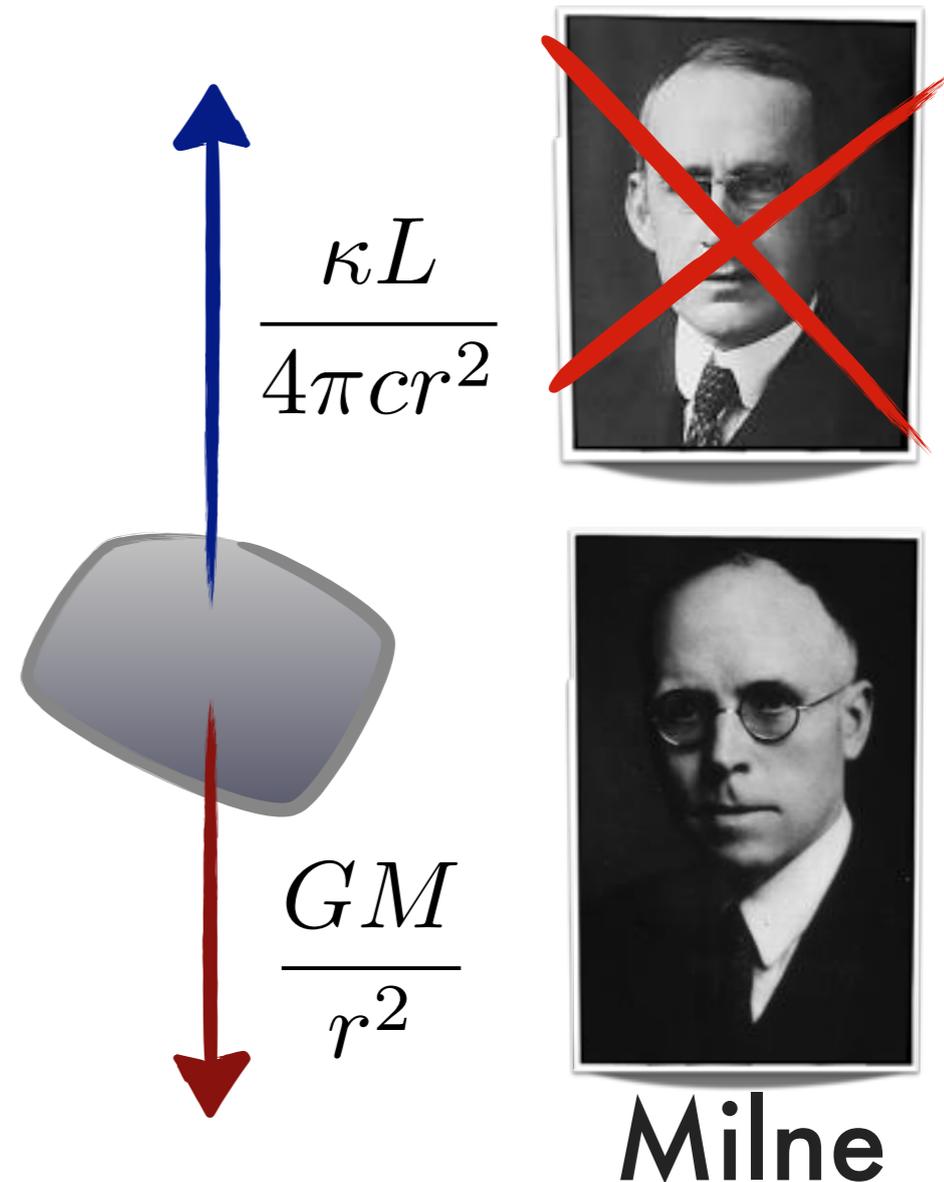
# The Eddington Limit

- The Eddington luminosity is the luminosity for which the **radiative force** balances the **gravitational pull**

$$L_{\text{edd}} = \frac{4\pi GMc}{\kappa}$$

- Note: For accretion disks effective area is larger, giving higher  $L_{\text{edd}}$ :

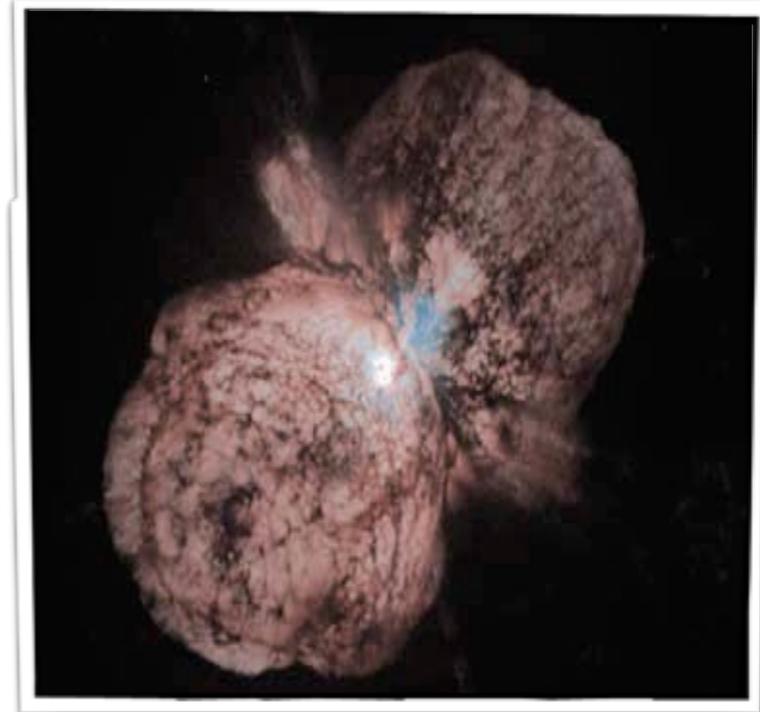
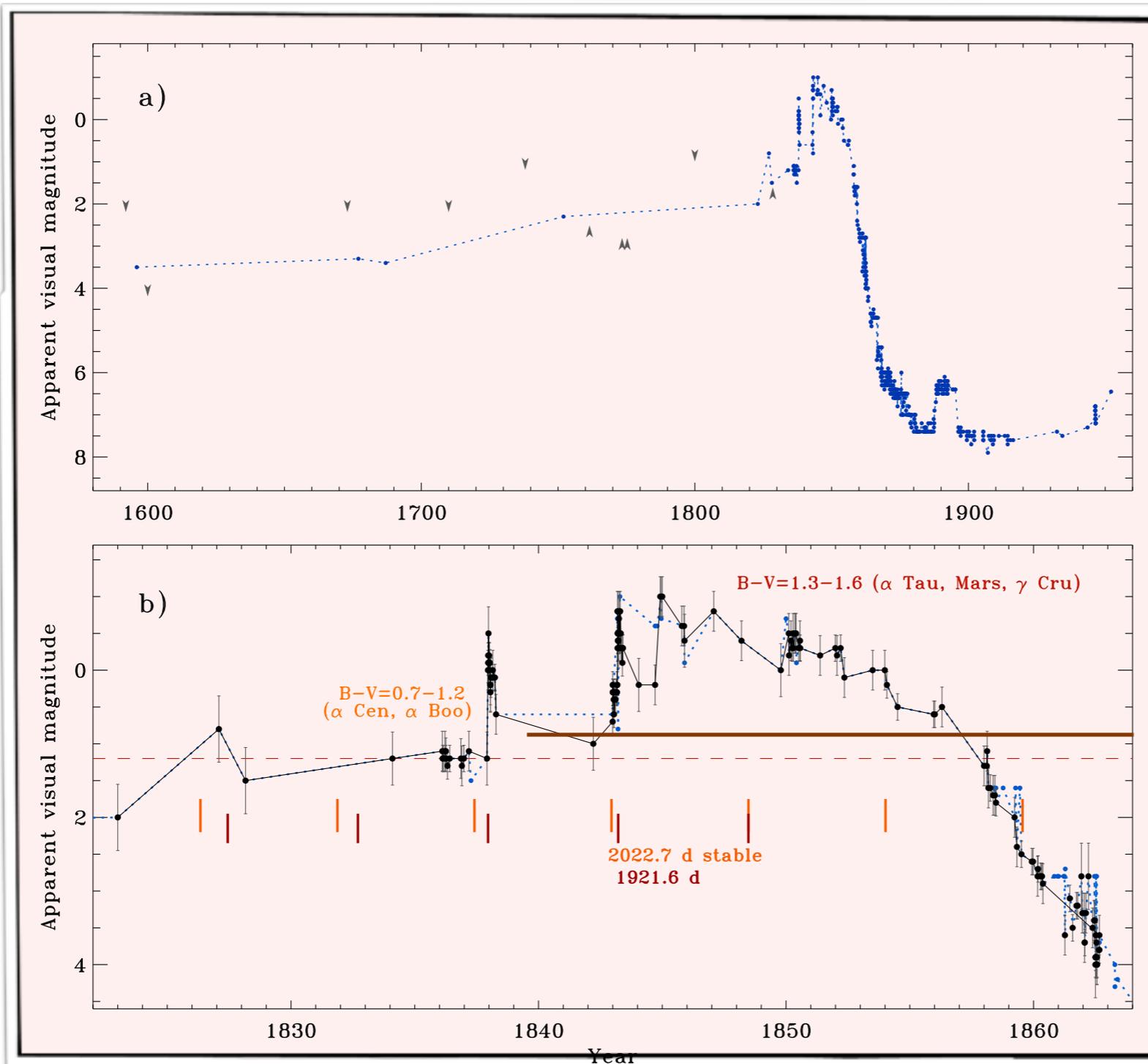
$$L_{\text{Edd,acc}} \approx \left( 1 + \ln \left( \frac{R_{\text{out}}}{R_{\text{in}}} \right) \right) L_{\text{Edd,Sph}}$$



# Why spherical objects first?

- Accretion disks are super-Interesting but more complicated than spherical objects
- We therefore study spherical objects first -  
Learn how super-Eddington systems behave
- Then apply to Accretion disks

# $\eta$ -Carinae - An LBV

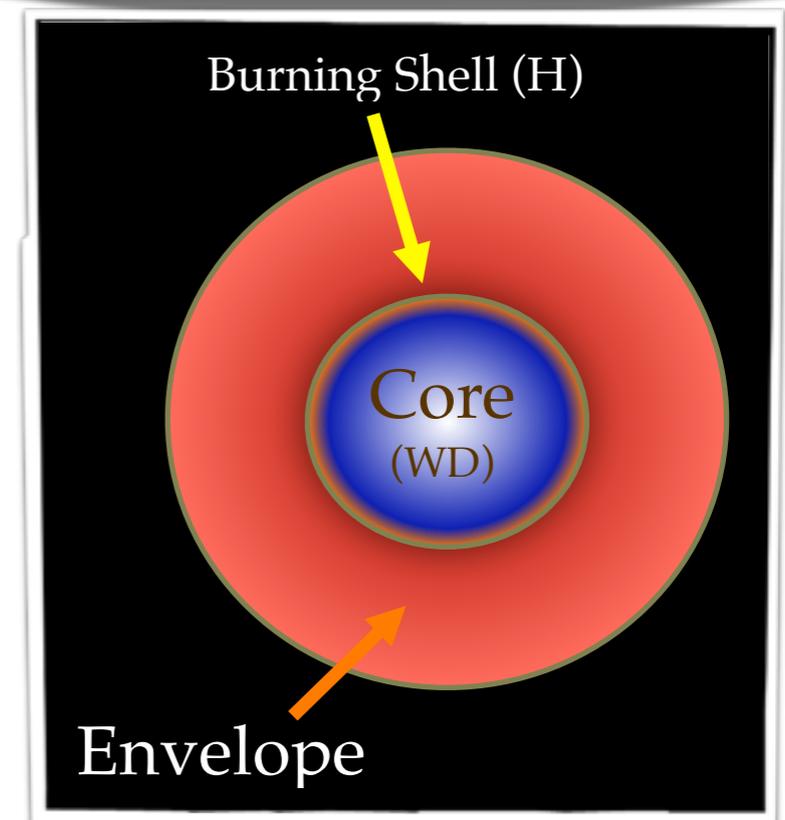
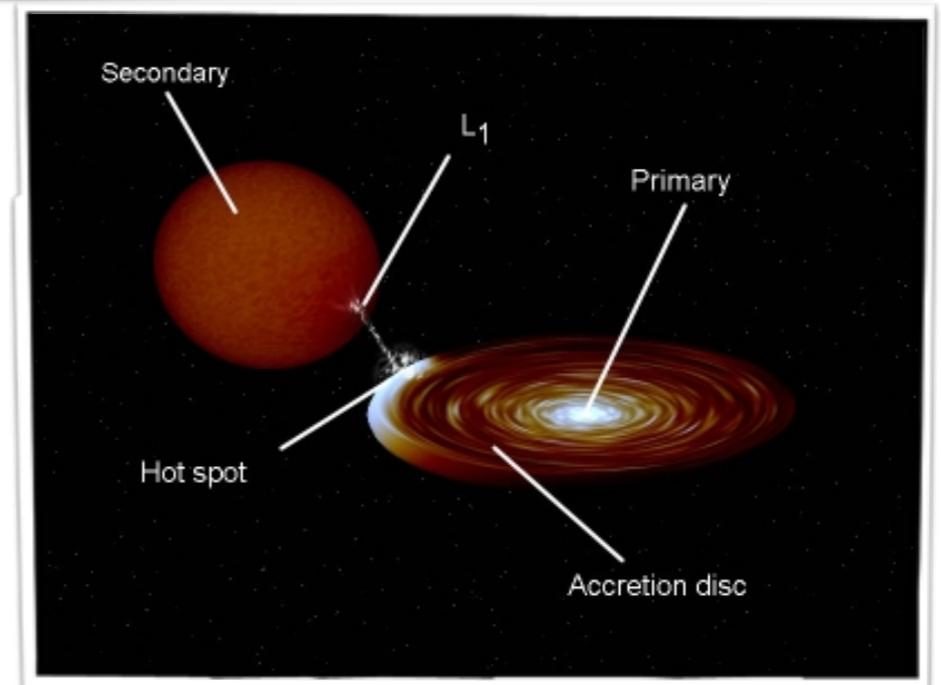


$$L_{\text{edd}}(M=150M_{\text{sun}} X=0.55)$$

Smith & Frew  
2010

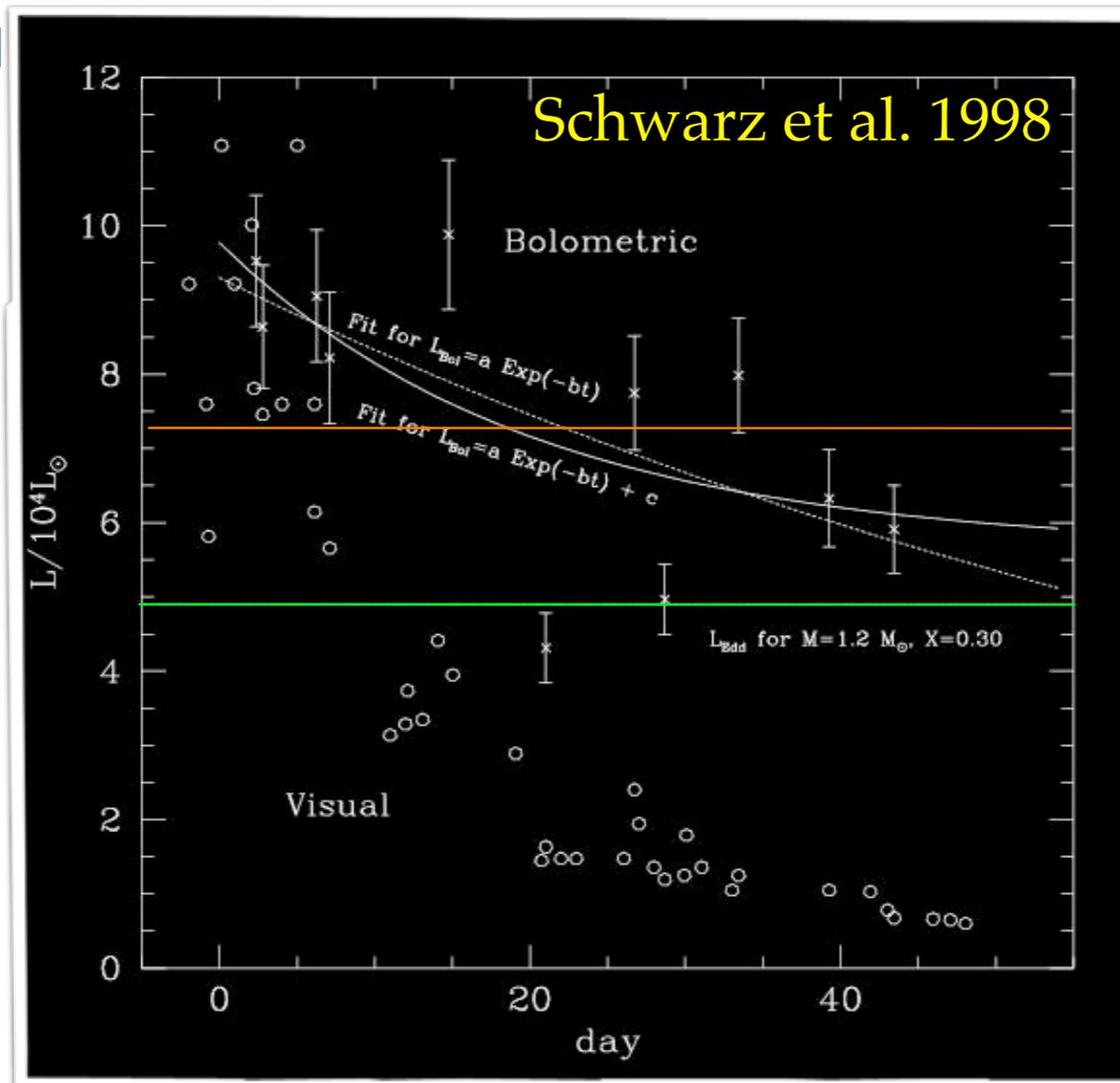
# Classical Novae

- When enough hydrogen is accreted on a white dwarf, it ignites.
- **Theory:** It should shine close to the Eddington limit (Paczynski 1970)
- **Reality:** Can be up to 20 times the  $L_{\text{Edd}}$ !



# Specific Novae Are Super-Eddington for a long time if observed in UV

Nova LMC 1988#1



Extreme  $L_{\text{edd}}$   
“upper limit”

( $M = 1.4 M_{\text{sun}}$ ,  $X = 0$ )

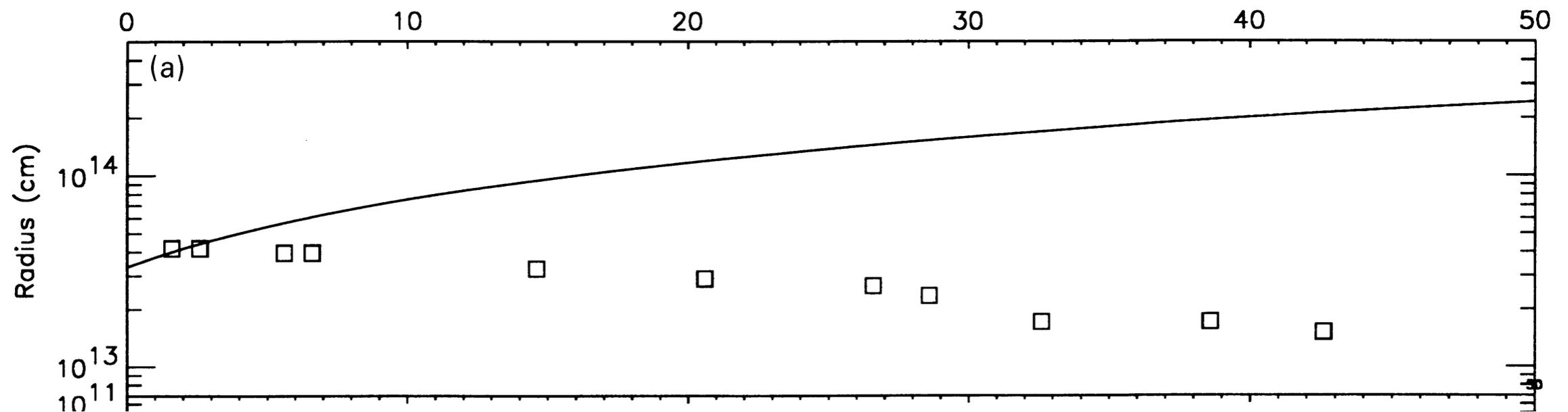
Reasonable  $L_{\text{edd}}$   
“upper limit”

( $M = 1.2 M_{\text{sun}}$ ,  $X = 0.3$ )

Photospheric radius  $\ll v t$

Nova LMC 1988#1

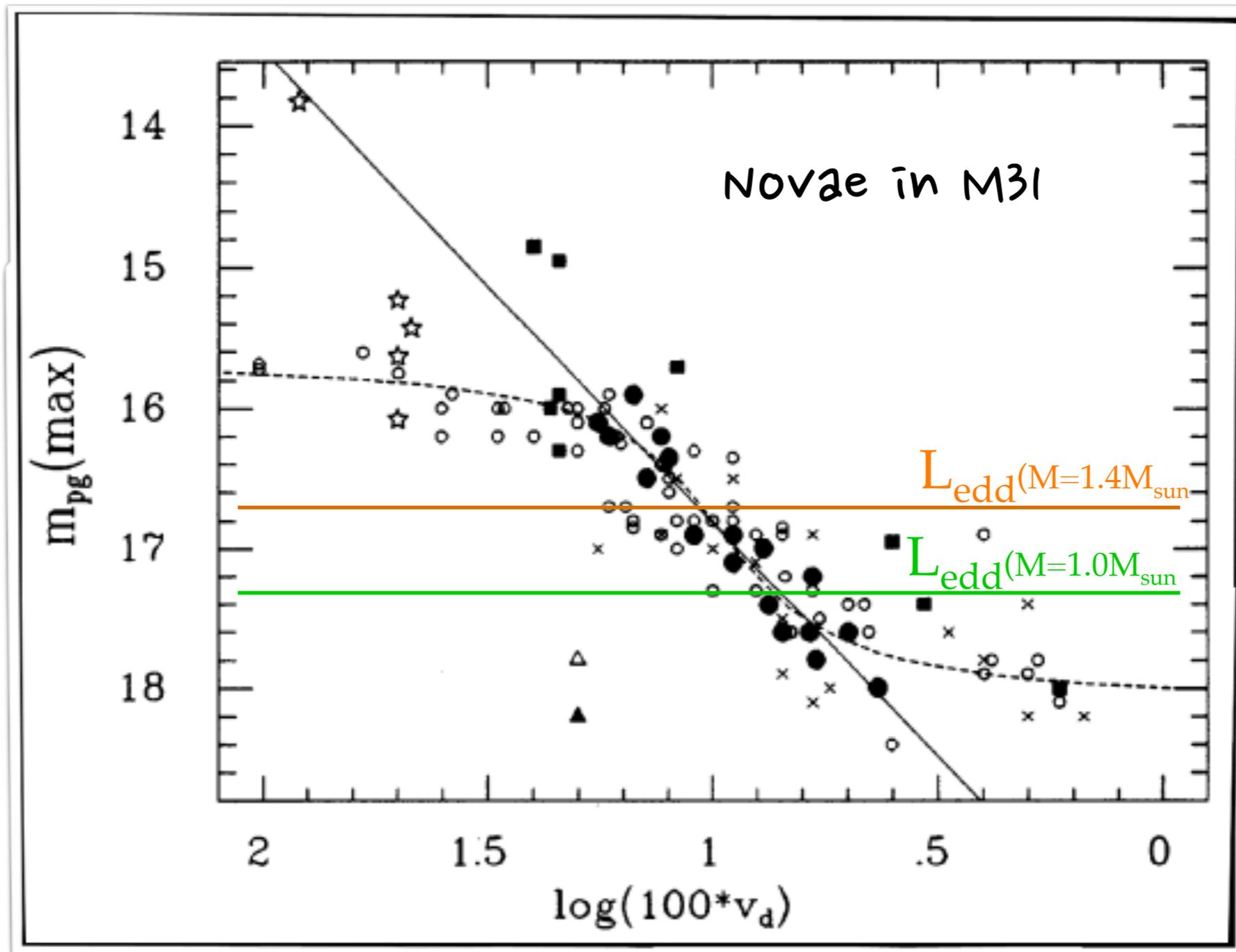
Schwarz et al. 1998



Novae have steady state winds with photospheres at  $r_{\text{sonic}} \ll r_{\text{ph}} \ll v t$  (Bath & Shaviv 1976)

Novae have steady state have steady super-Eddington continuum driven winds (Shaviv 2001)

# Peak Luminosity of Classical Novae is super-Eddington

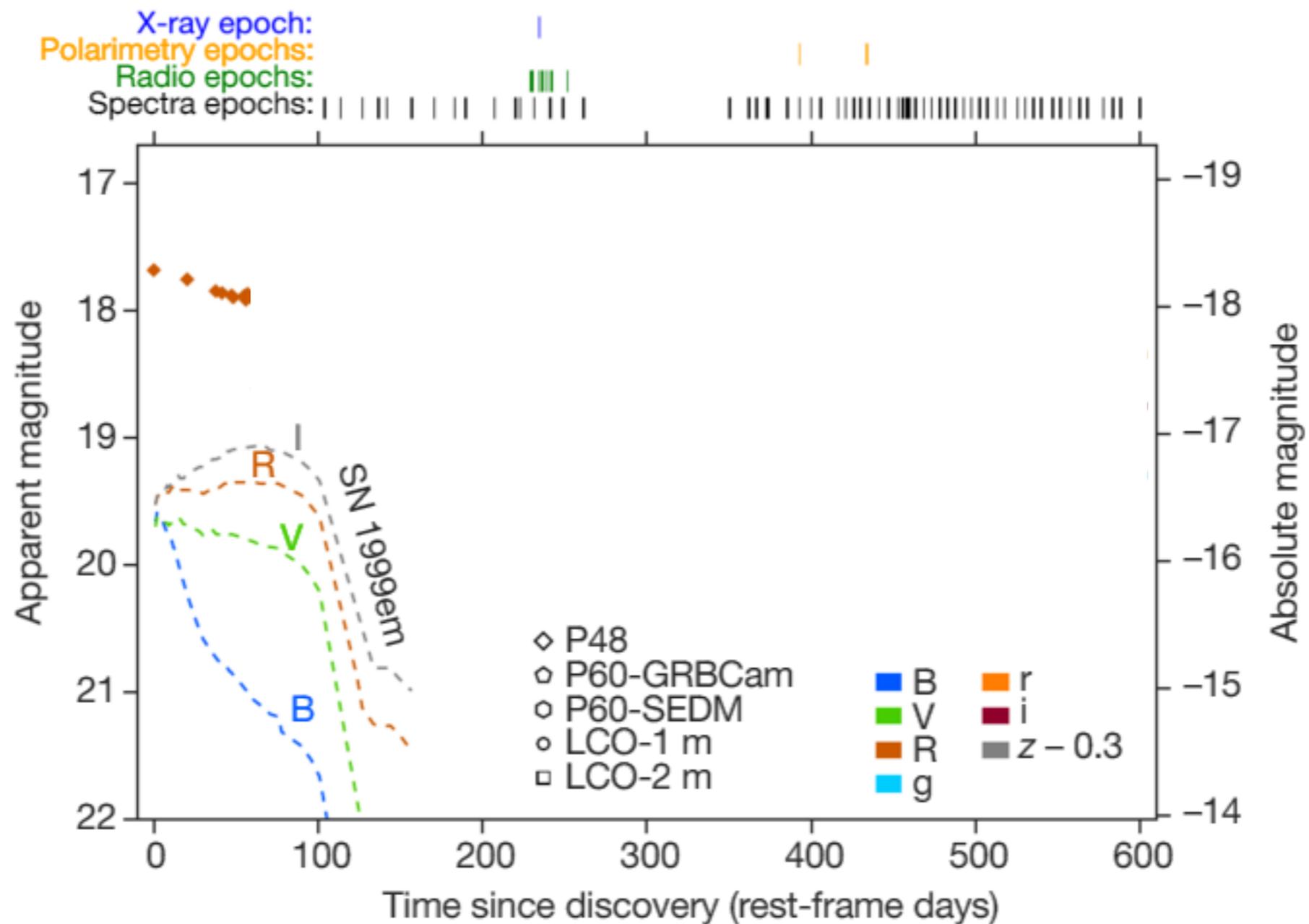


( $v_d$  = rate of decline in mags/days =  $2 / t_2$ )

Capaccioli et al. 1989

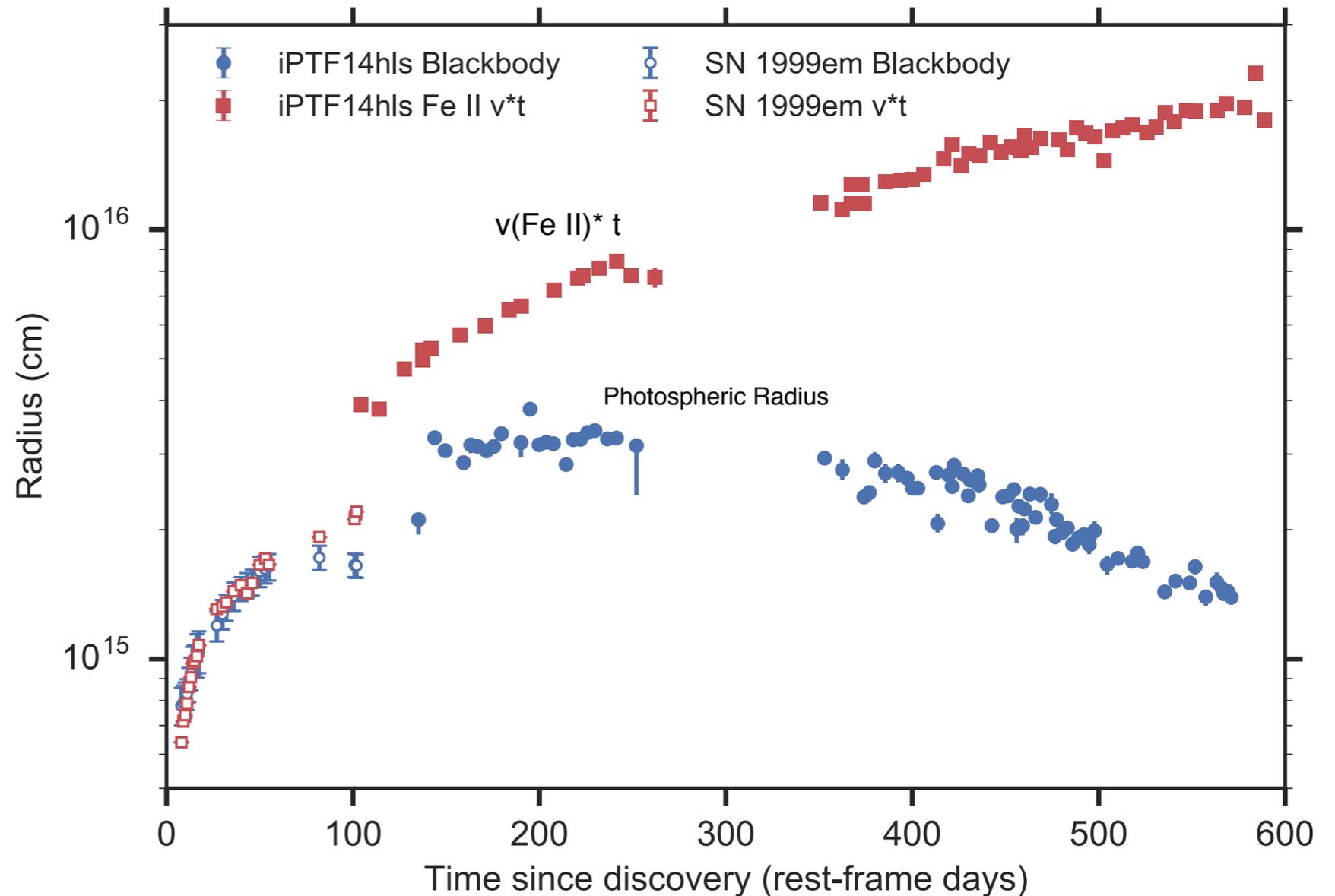
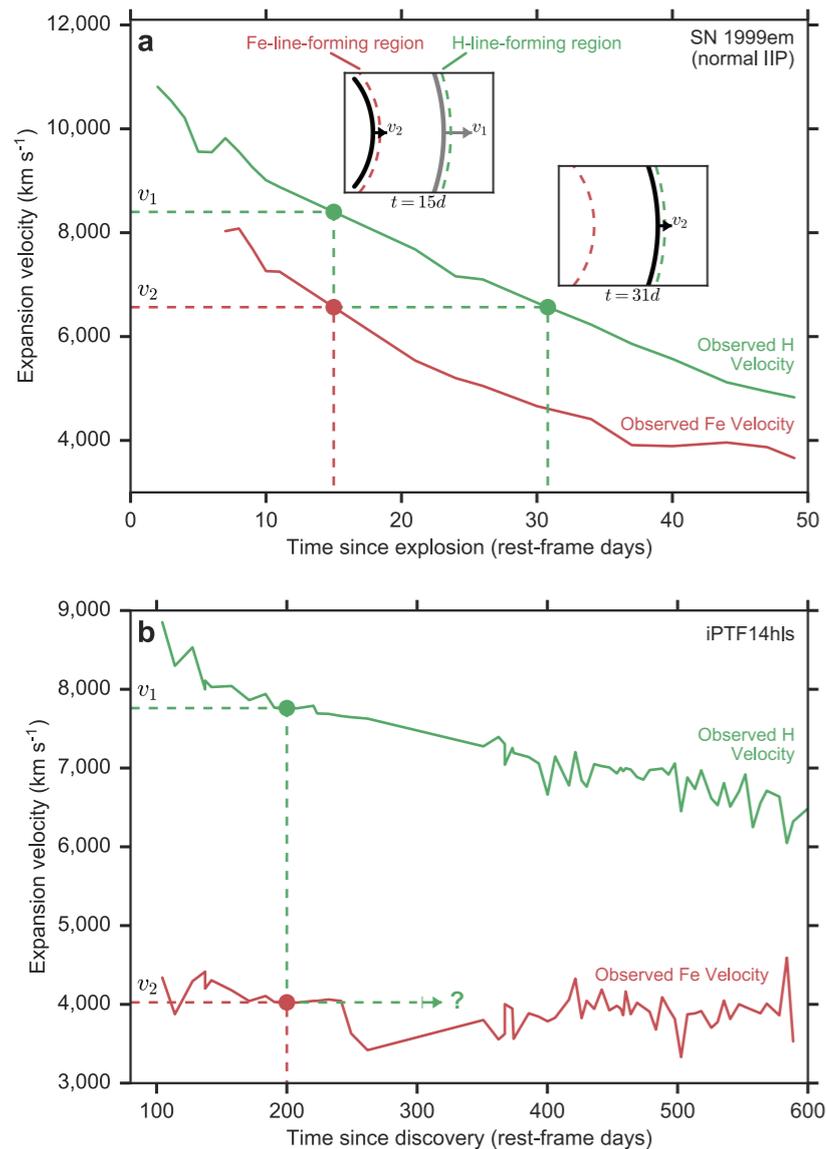
# iPTF14hls

- A supernova?



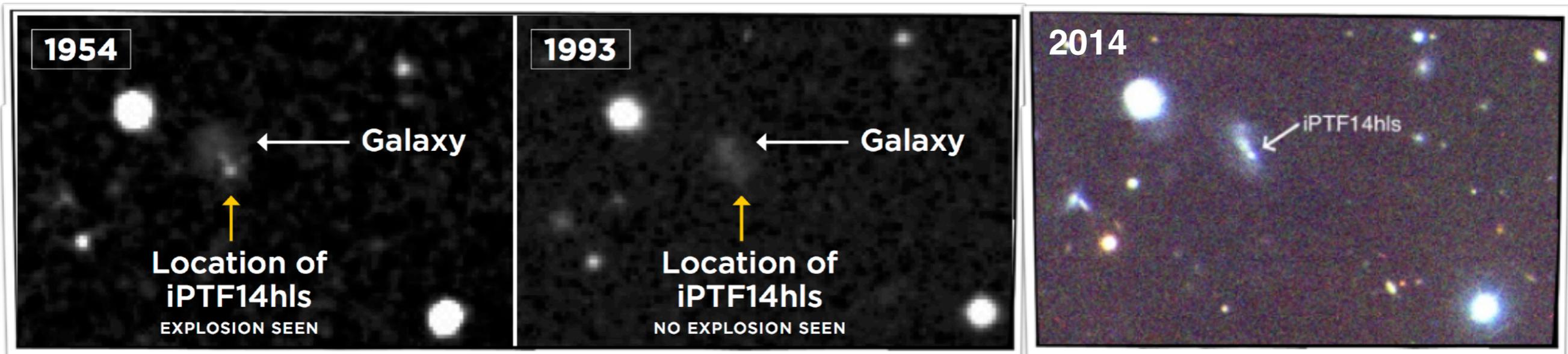
# iPTF14hls

- Not a supernova, it has a steady state wind  $r_{ph} \ll v t$



# iPTF14hls

- Not a supernova, it is also episodic



Mv ~ -15.5

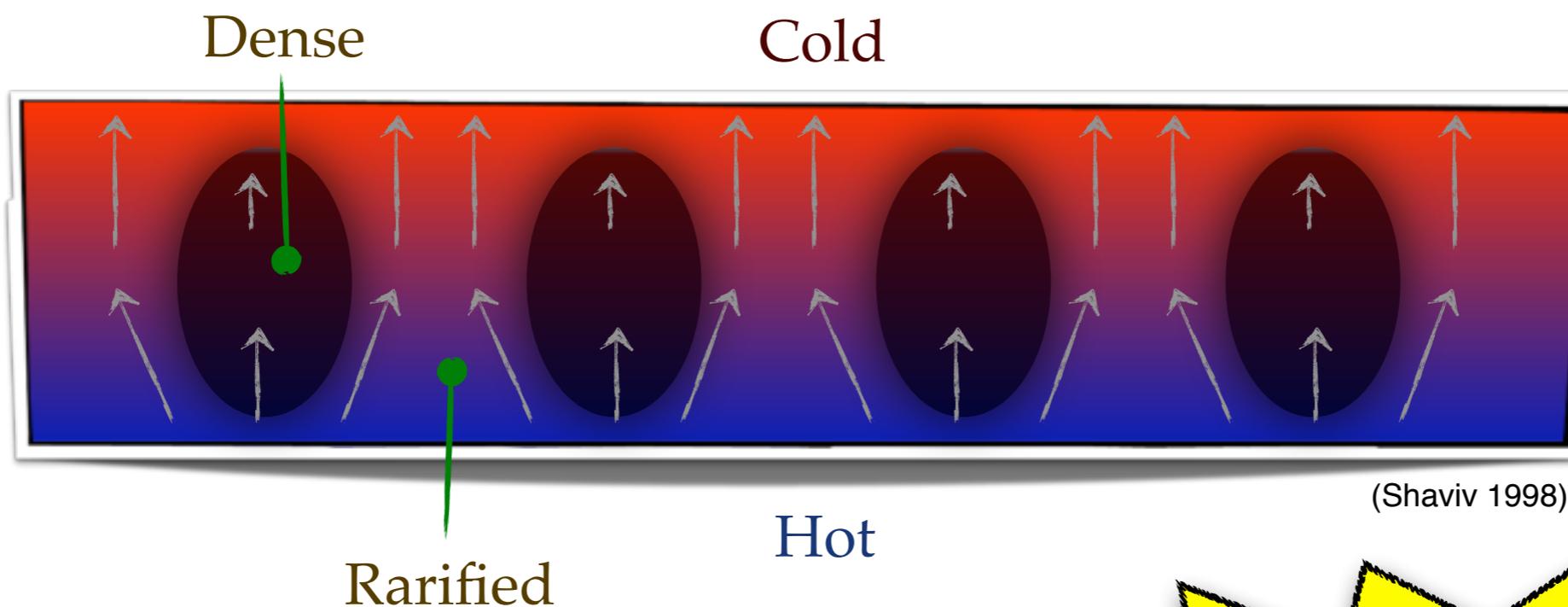
Mv ~ -18.5  
500 Ledd of 100 Msun!

# super-Edd in Nature

- LBV Giant Eruptions
- Classical Nova eruptions
- Type IIIn (and Ibn) precursors
- Post failed-SN lax winds from WD remnant
- ULXs (which are not IMBH...)

# How can objects be super-Eddington?

- **Secret:** Atmospheres are porous



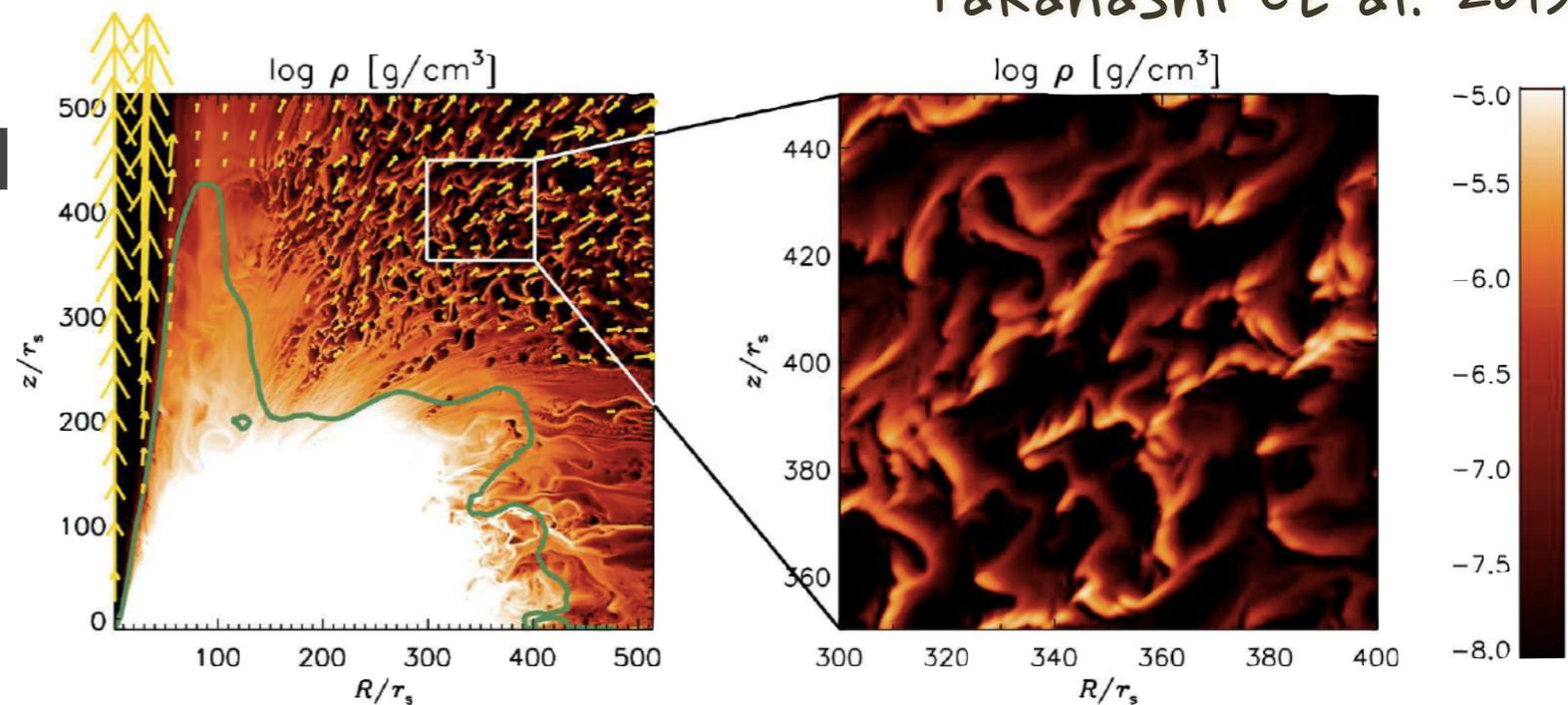
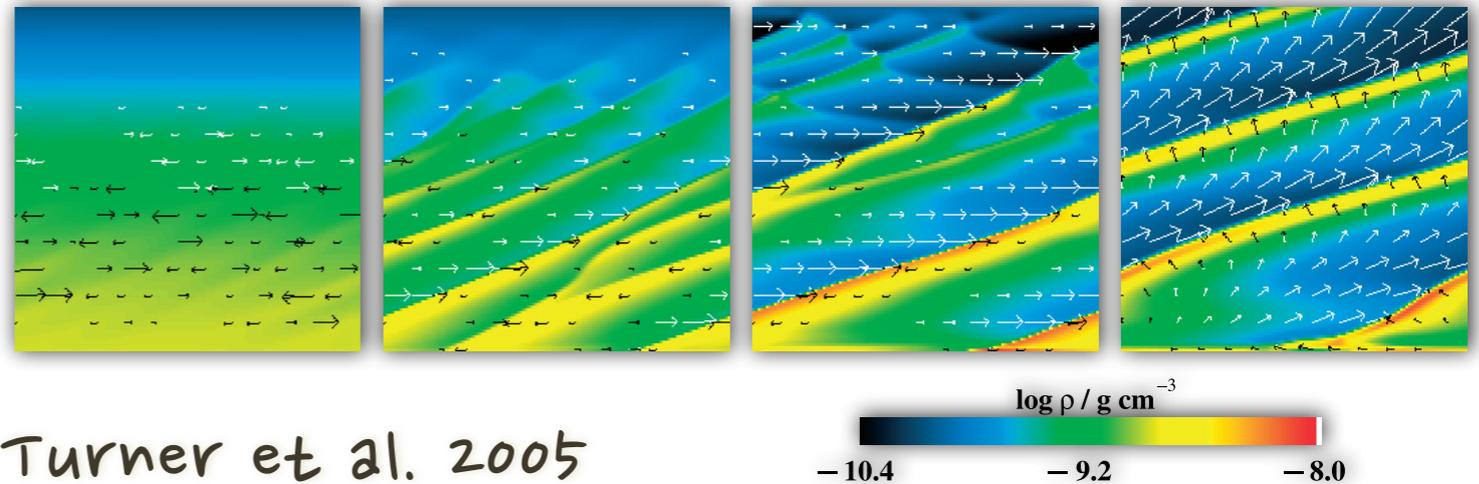
On average, the radiation "sees" a smaller opacity (per unit volume)

$$\kappa_V^{\text{eff}} = \frac{\langle F \kappa_V \rangle_V}{\langle F \rangle_V}$$

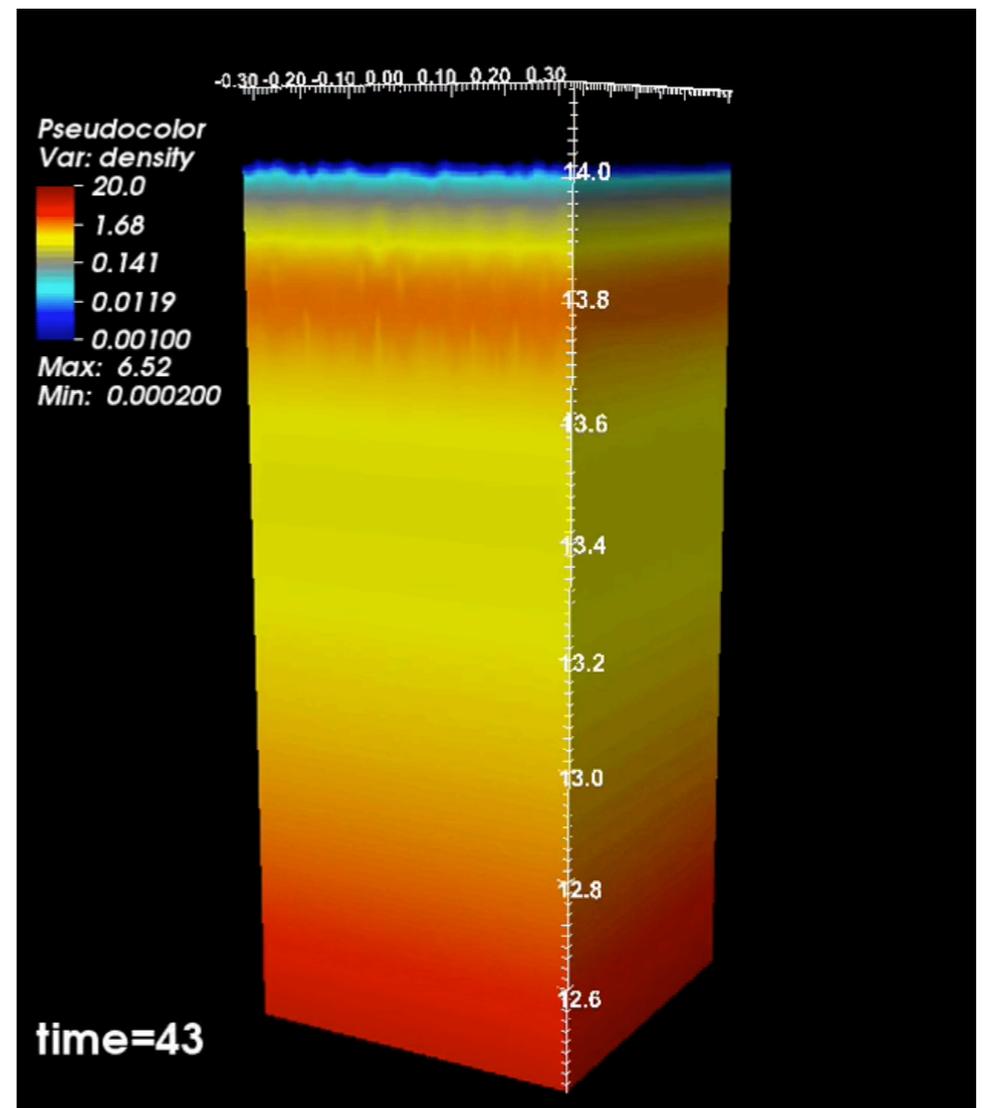
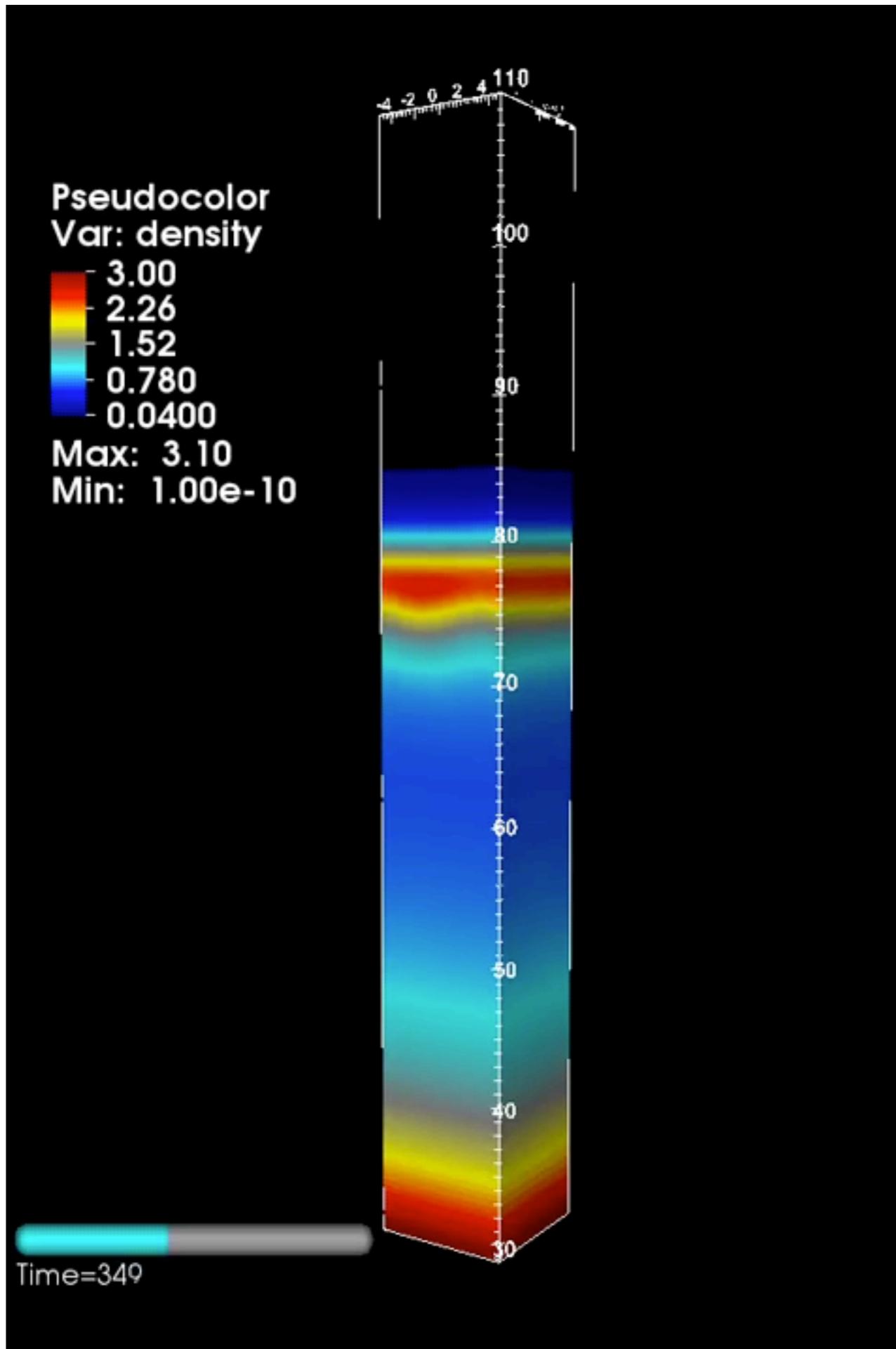
NJS 1998

# Instabilities close to $L_{\text{edd}}$

- There are many radiative hydrodynamic instabilities under various conditions
- Radiation + Hydro + stratification (NJS, 2001)
- Radiation + B-field (Arons '92, Hsu et al. '97, Gammie '98, Blaes & Socrates '01, Begelman '01)
- s-mode instability under special opacity laws (Glatzel 1994; Papaloizou et al. 1997)



Instabilities close to  $L_{\text{edd}}$



# Full Picture

▶ Atmospheres are **unstable** as they approach the Eddington Luminosity

▶ Atmospheres become Inhomogeneous

▶ Effective Opacity is Reduced

▶ **Effective** Eddington Luminosity is Increased

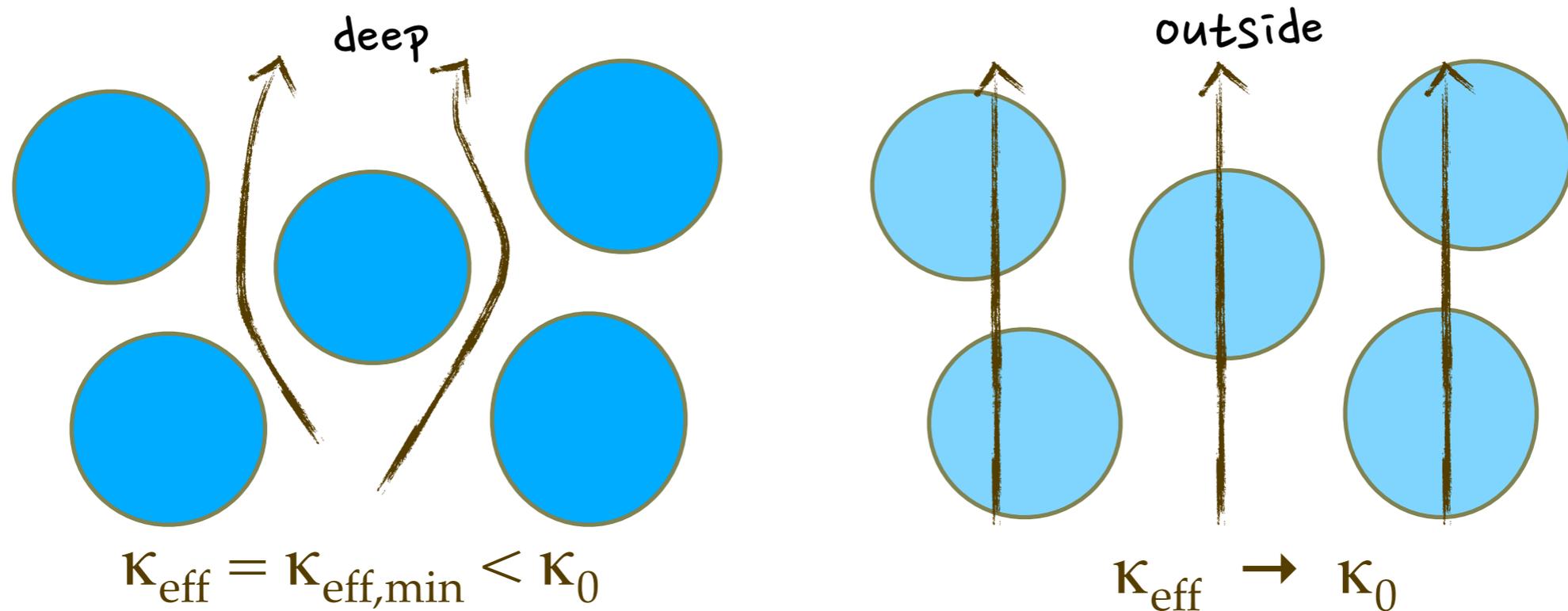
What do these atmospheres look like?

“...The answer my friends, is blowing in the wind,  
the answer is blowing in the wind...”



# Wind from super-Edd Atmospheres

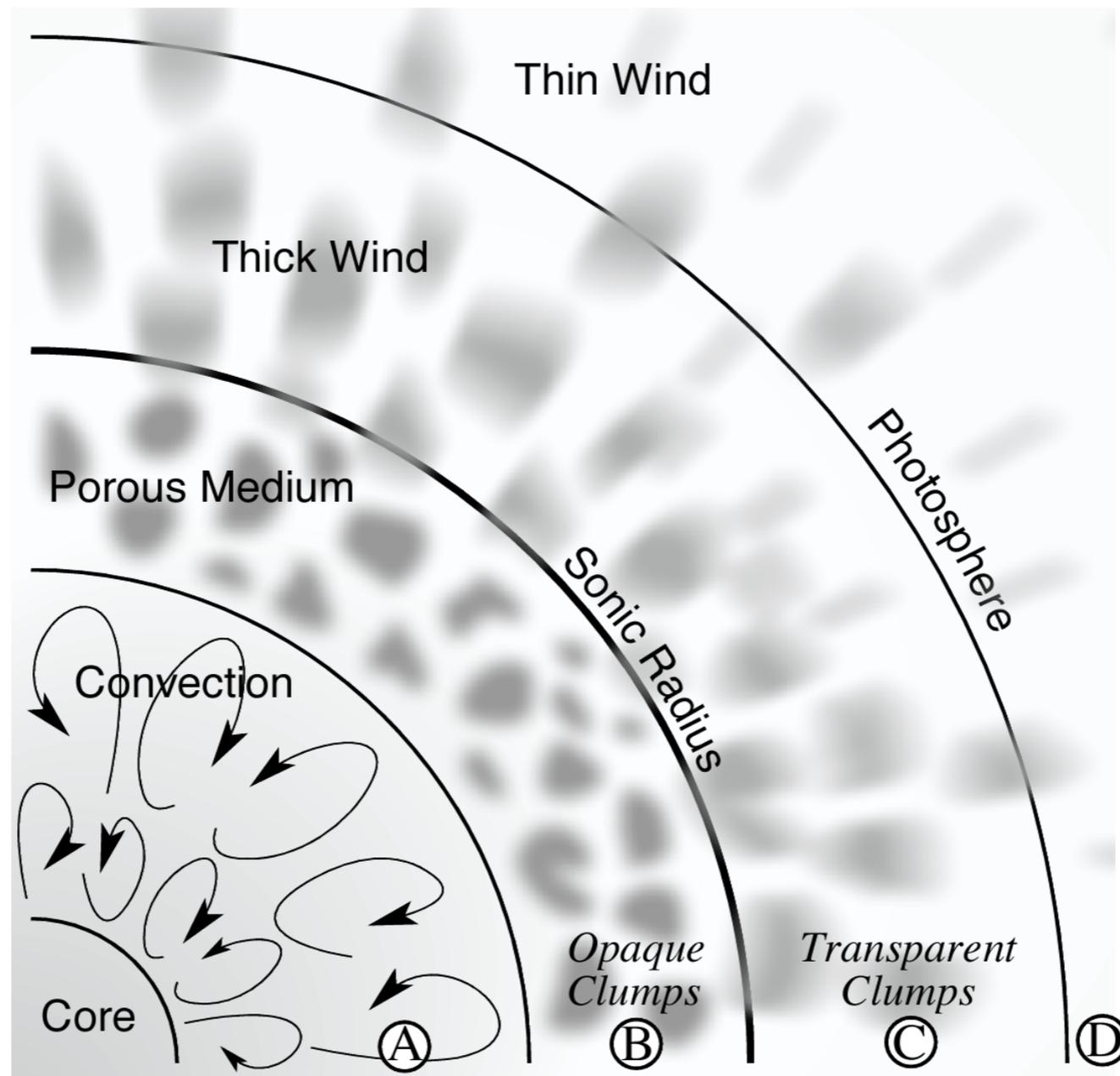
- Theory predicts wind from region where structure becomes optically thin (transparent)



$$\dot{m} = \mathcal{W} \frac{(L - L_{\text{Edd}})}{v_s c}$$

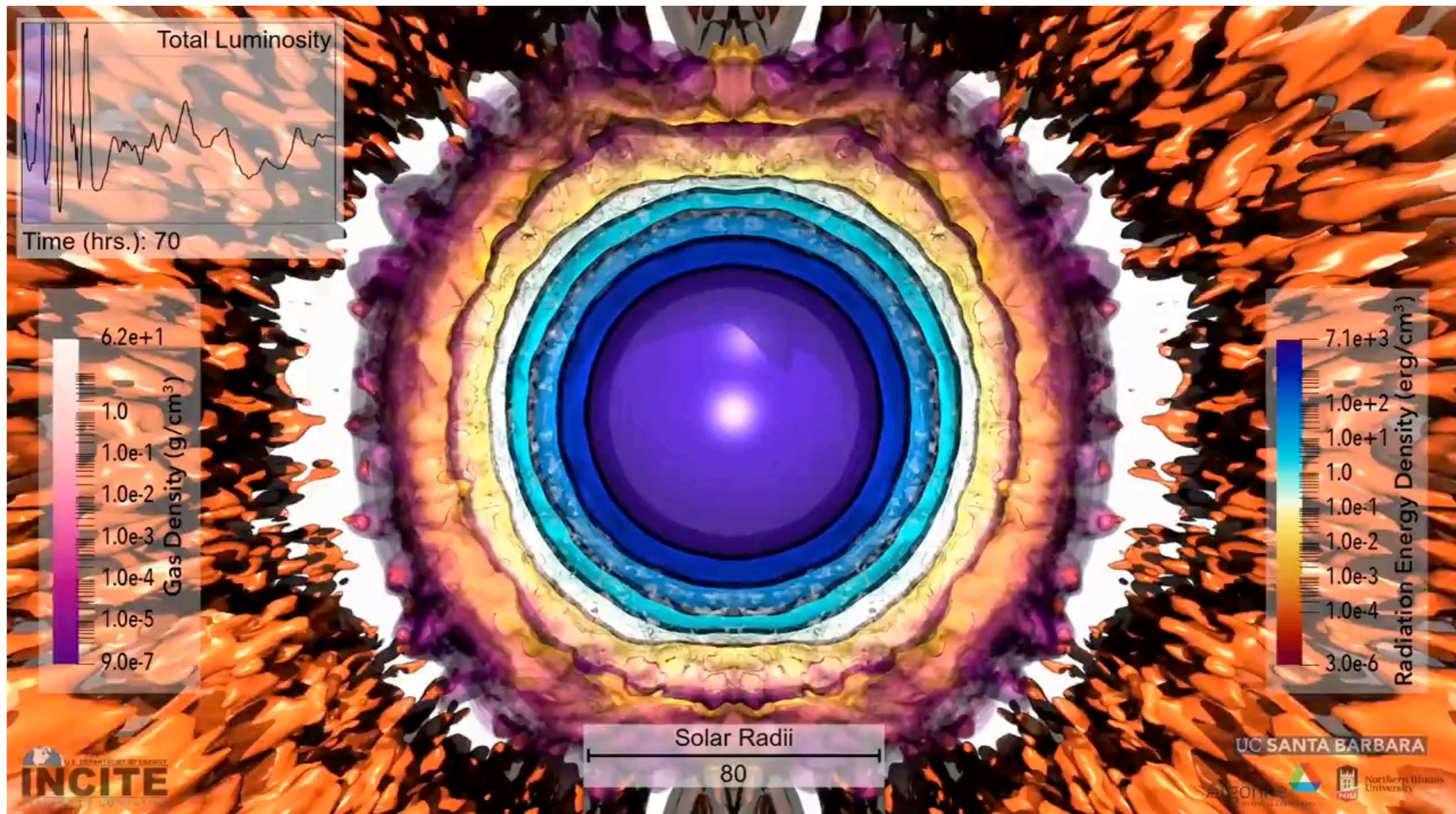
# Structure of Porous atmospheres

- Prediction:

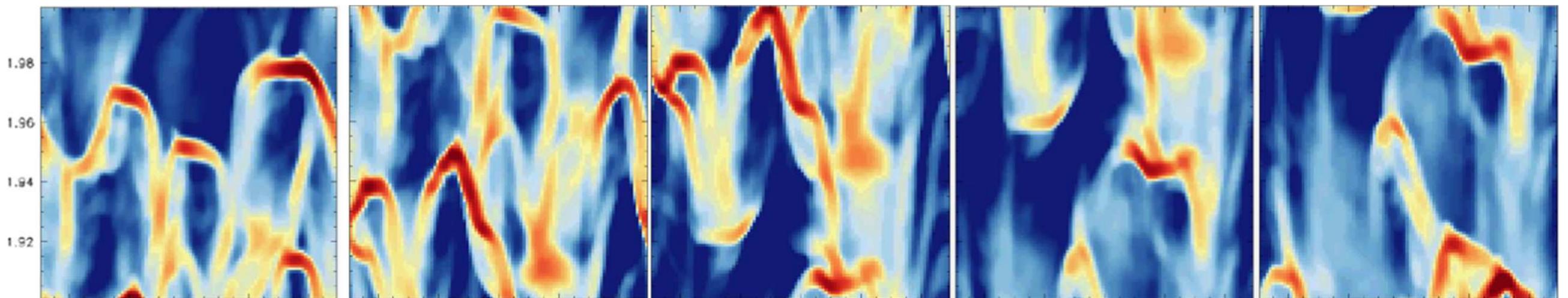
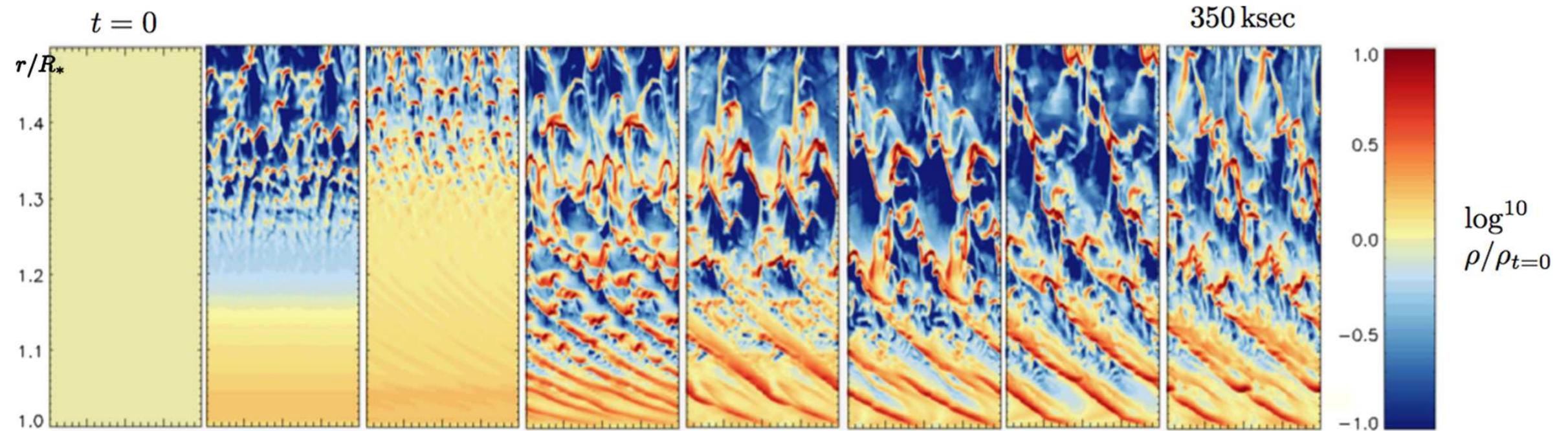


# Structure of Porous atmospheres

- 18 years later + 7000 CPU years (!)

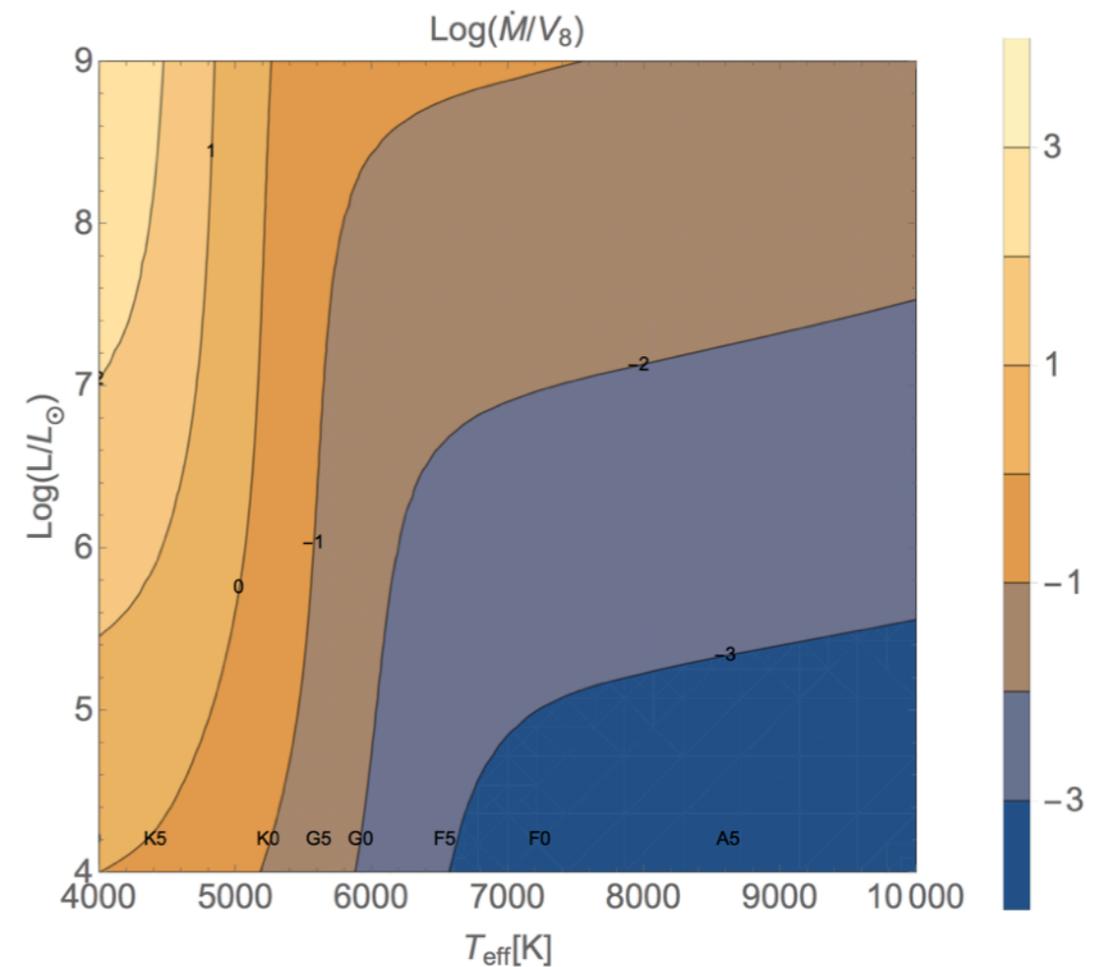
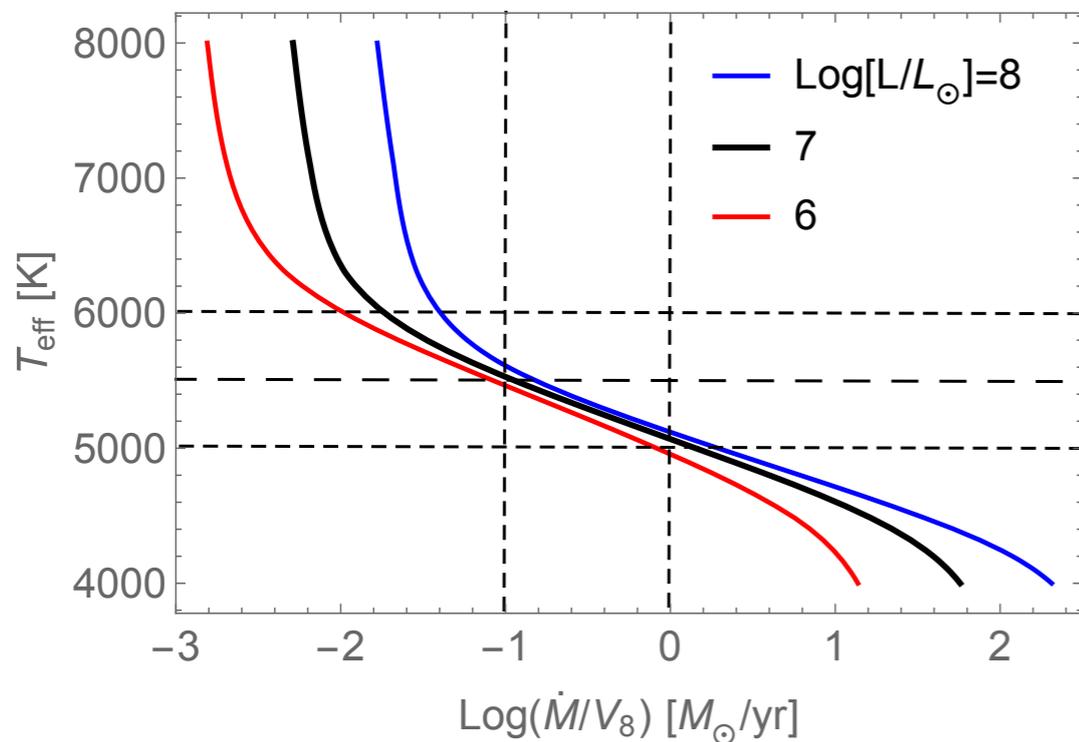


# Note: Winds are also unstable



# photospheres

- In optically thick winds, the photosphere resides in the wind. (Bath & Shaviv 1976)
- For m-dots seen in  $\eta$  Car: One expects  $T_{\text{eff}} \sim 5000\text{K}$
- This is seen in the light echo (Rest et al. 2012).



# The Winds

- Given photospheric conditions ( $L$ ,  $v$ ,  $\dot{m}$  or  $T_{\text{ph}}$ ,  $M$ ) we can integrate down until we reach the sonic radius.

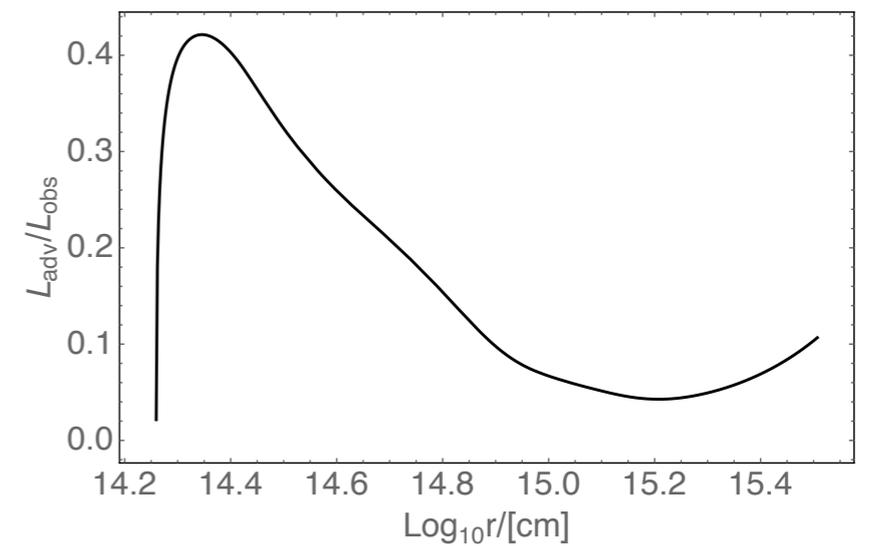
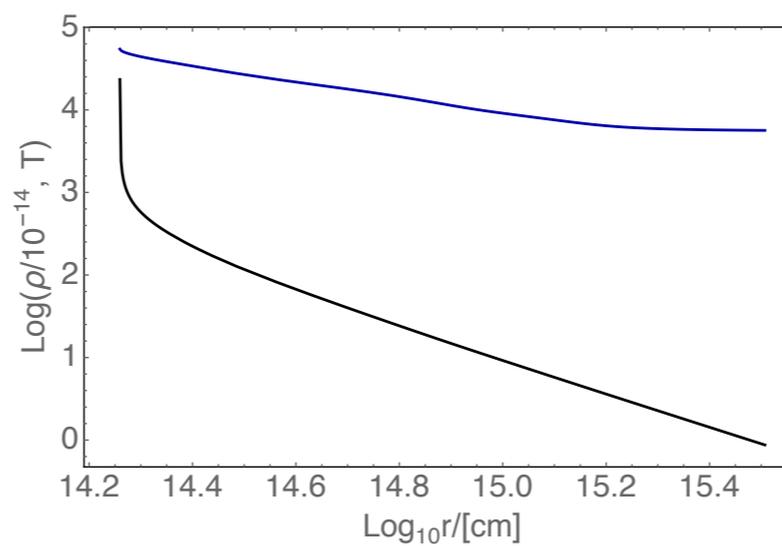
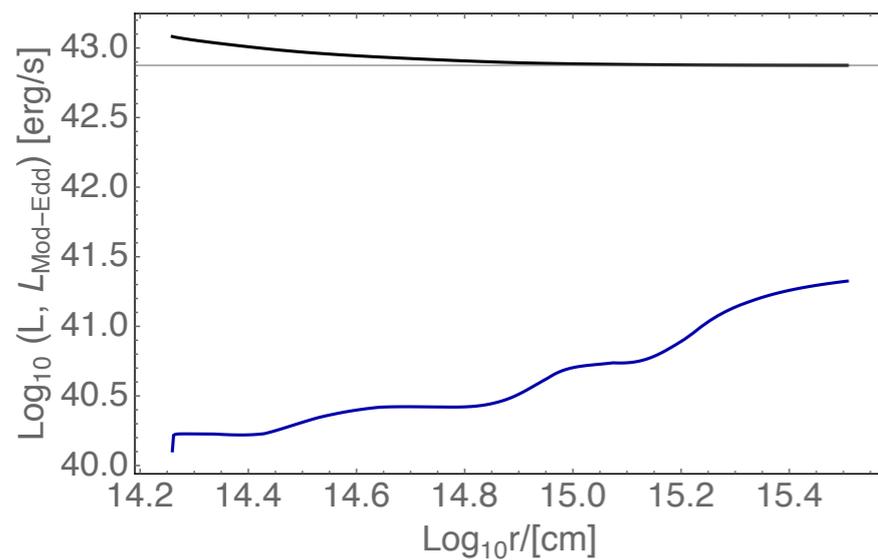
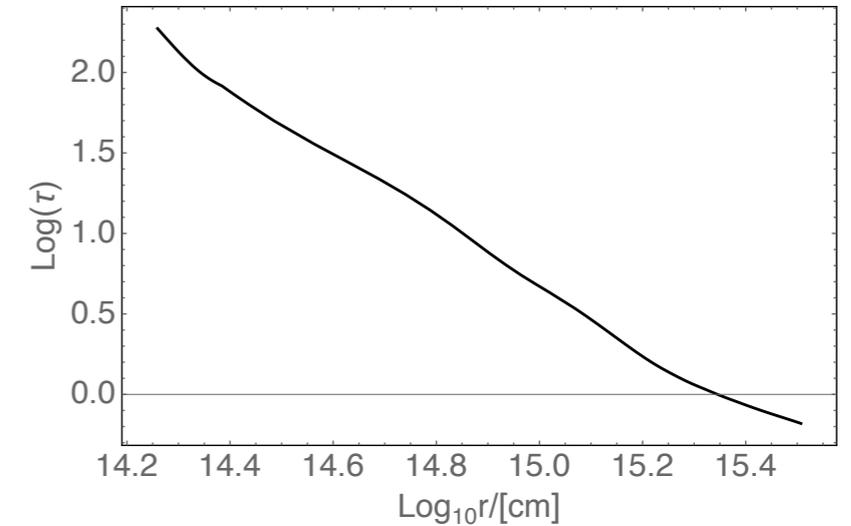
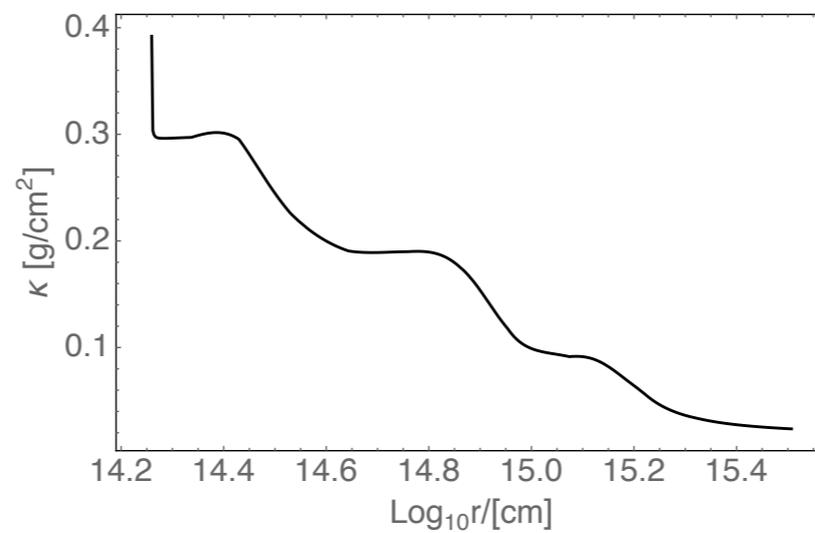
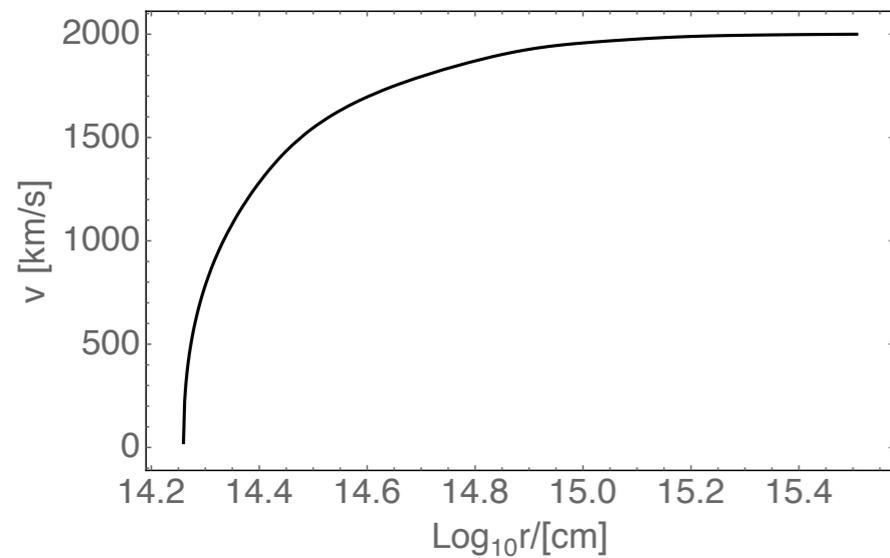
$$\dot{M} = 4\pi\rho v r^2$$

$$v \frac{dv}{dr} = \frac{\kappa}{c} \left( \frac{L}{4\pi r^2} - 4v P_{\text{rad}} \right) - \frac{GM}{r^2} - \frac{1}{\rho} \frac{dP}{dr}$$

$$\frac{d}{dr} [\dot{M}(v^2/2 + h_g - GM/r) + L] = 4\pi r^2 \dot{q}$$

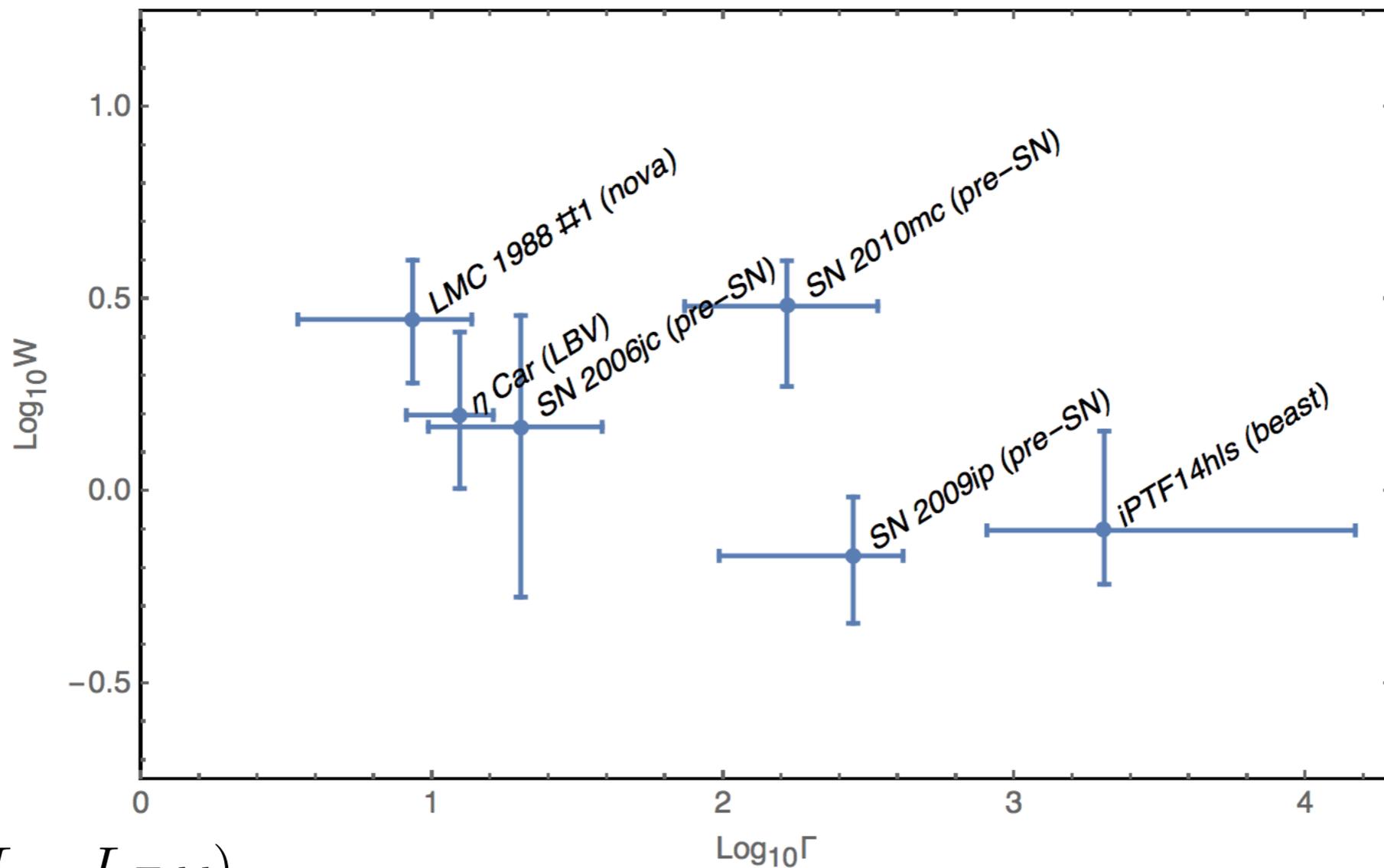
$$\frac{dP_{\text{rad}}}{dr} = -\frac{\rho\kappa}{c} \left( \frac{L}{4\pi r^2} - 4v P_{\text{rad}} \right),$$

# e.g., solution for iPTF14hls



# Empirically obtaining $\mathcal{W}(\Gamma)$

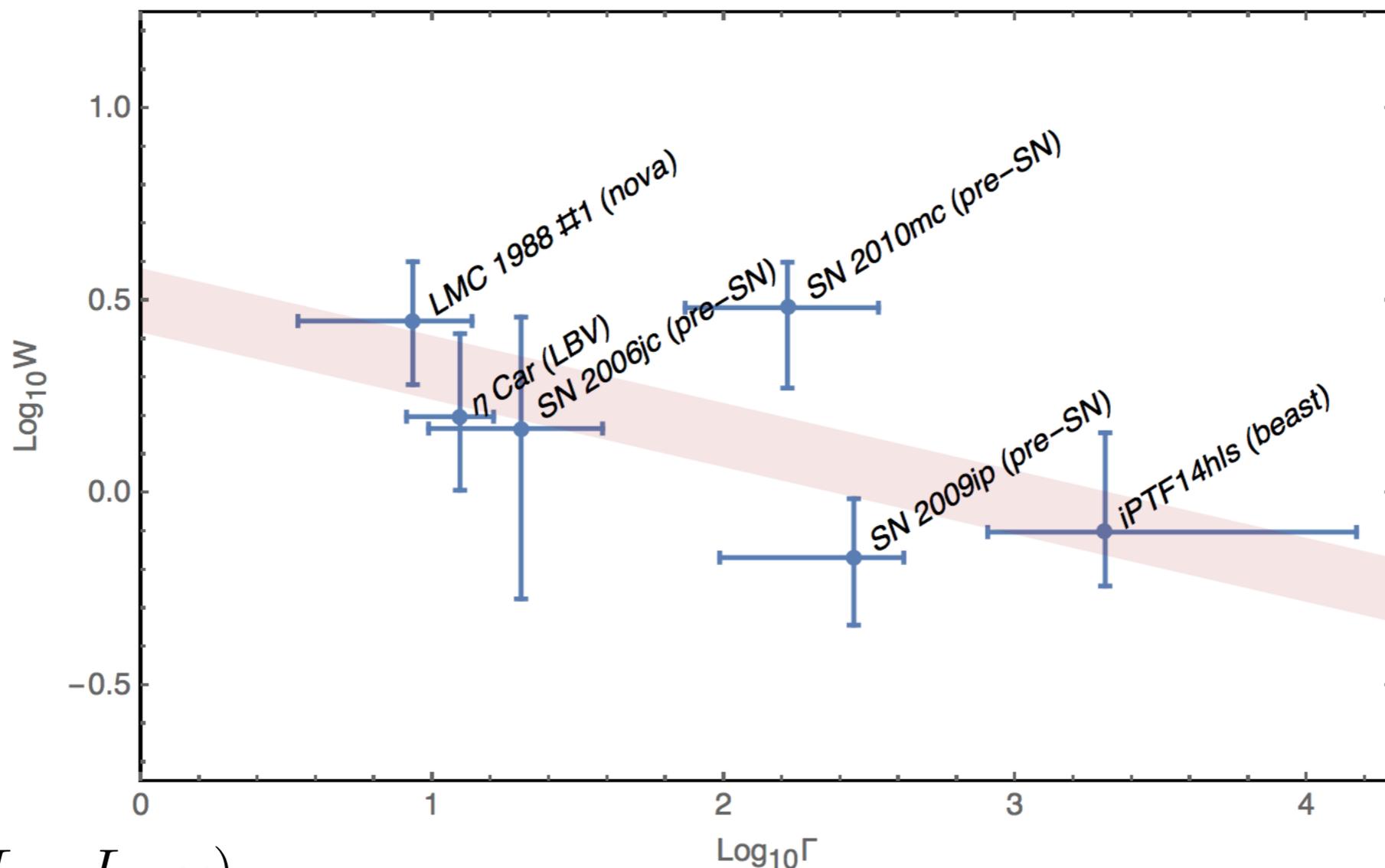
- $\mathcal{W}$  is expected to be  $O(1)$ , and slowly falling with  $\Gamma$  (higher  $\Gamma$ , more nonlinear structure, lower effective opacity).



$$\dot{m} = \mathcal{W} \frac{(L - L_{Edd})}{v_s c}$$

# Empirically obtaining $\mathcal{W}(\Gamma)$

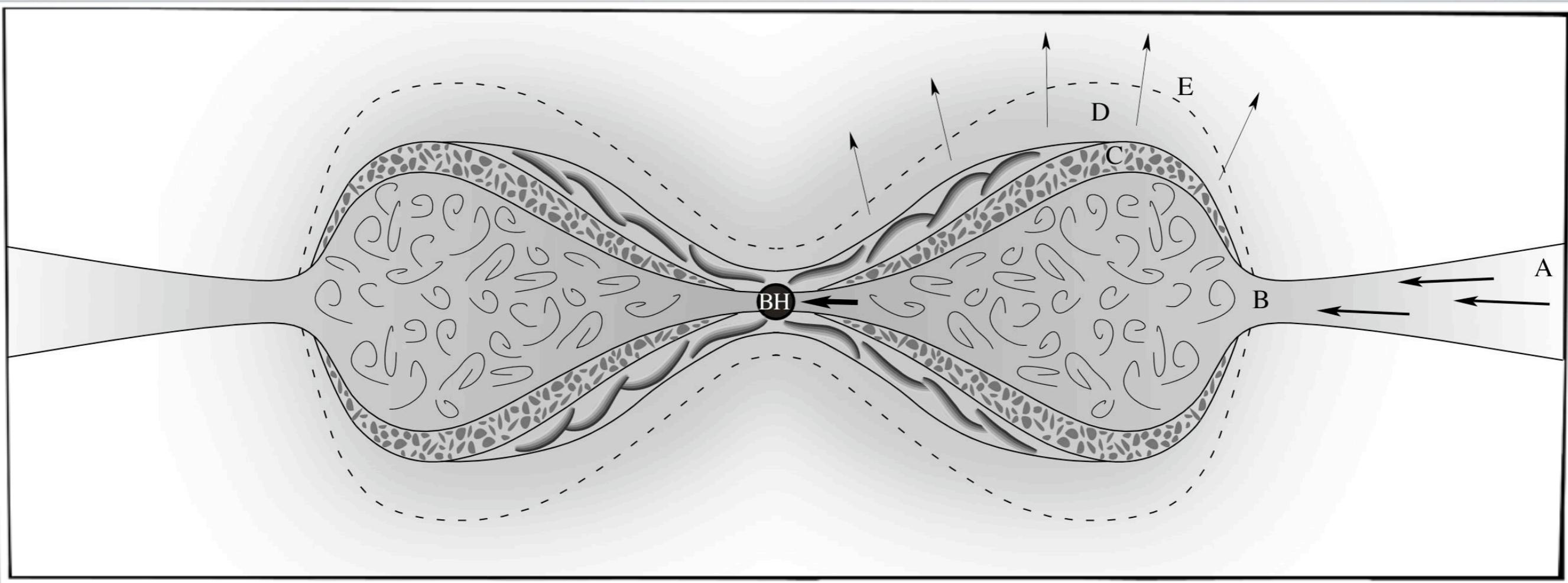
- $\mathcal{W}$  is expected to be  $O(1)$ , and slowly falling with  $\Gamma$  (higher  $\Gamma$ , more nonlinear structure, lower effective opacity).



$$\dot{m} = \mathcal{W} \frac{(L - L_{Edd})}{v_s c}$$

$$\mathcal{W} \sim 3 \Gamma^{-1/6}$$

# Application to Accretion Disks



# Radial Structure: Equations

- Mass conservation,

$$\frac{d\dot{m}}{dr} = 4\pi r \dot{\Phi}_{\text{wind}}$$

- Radial momentum,

$$v_r \frac{dv_r}{dr} + \frac{1}{\rho} \frac{dP}{dr} = -\frac{\partial \Psi}{\partial r}$$

- Pseudo-Newtonian potential

$$\Psi = -\frac{GM_{\text{BH}}}{R - rg} \quad R = \sqrt{r^2 + z^2}.$$

# Radial Structure

- Angular momentum,

$$\rho v_r \frac{d}{dr} (r^2 \omega) = -\frac{1}{r} \frac{d}{dr} (r^2 \tau_{r\phi}) \quad \tau_{r\phi} = -\alpha P_{\text{tot}}$$

- Advection,

$$T \frac{ds}{dr} = (F - \phi) \frac{4\pi r}{\dot{m}}$$

# Vertical Structure: Hydrostatic region

- Hydrostatic equilibrium,

$$\frac{1}{\rho} \frac{dP}{dz} = - \frac{d\Psi}{dz}$$

- Temperature gradient ,

$$\frac{dT}{dz} = \begin{cases} \frac{\gamma - 1}{\gamma} \frac{dP}{dz} \frac{T}{P}, & \text{in the convective zone,} \\ - \frac{3\kappa_{\text{eff}} \rho F}{4acT^3}, & \text{in the radiative zone,} \end{cases}$$

# Vertical Structure: Porous Atmosphere

- The effective opacity is

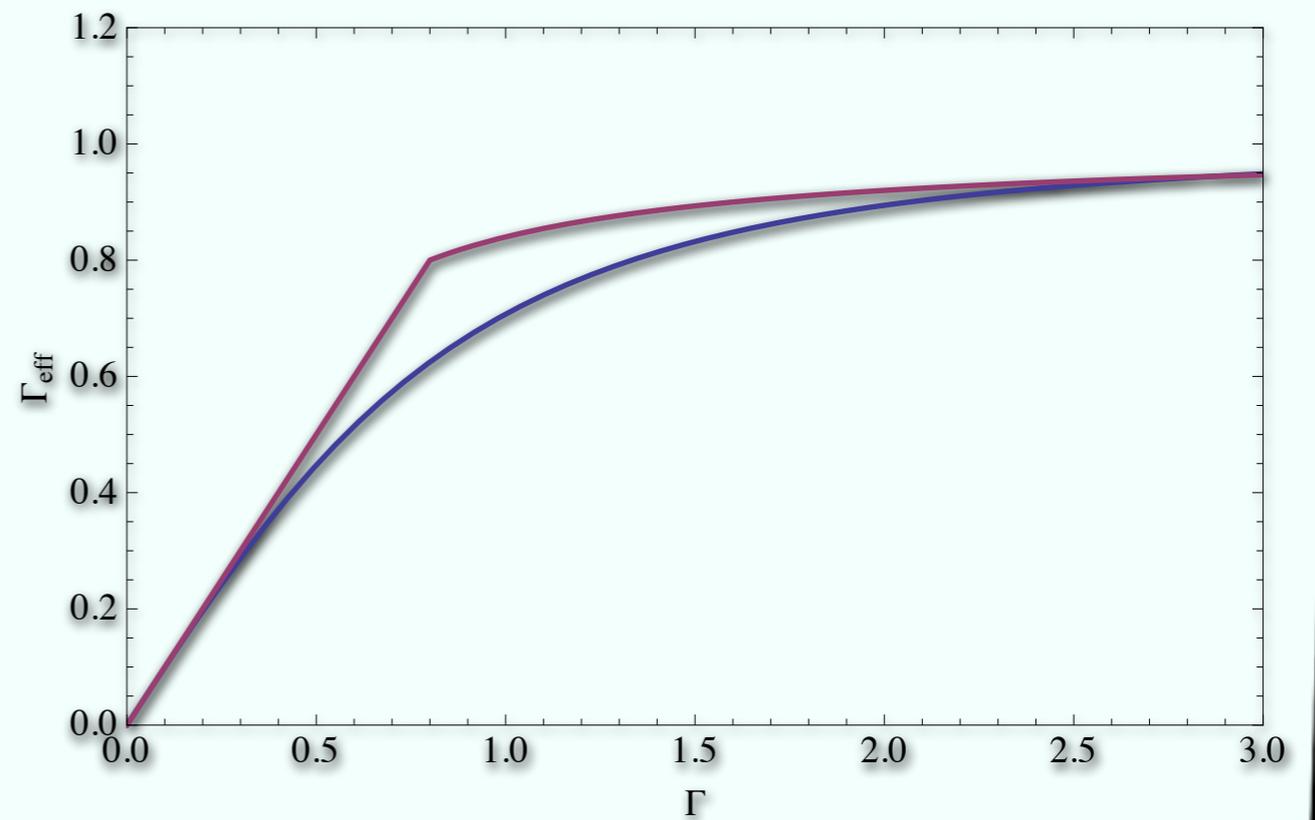
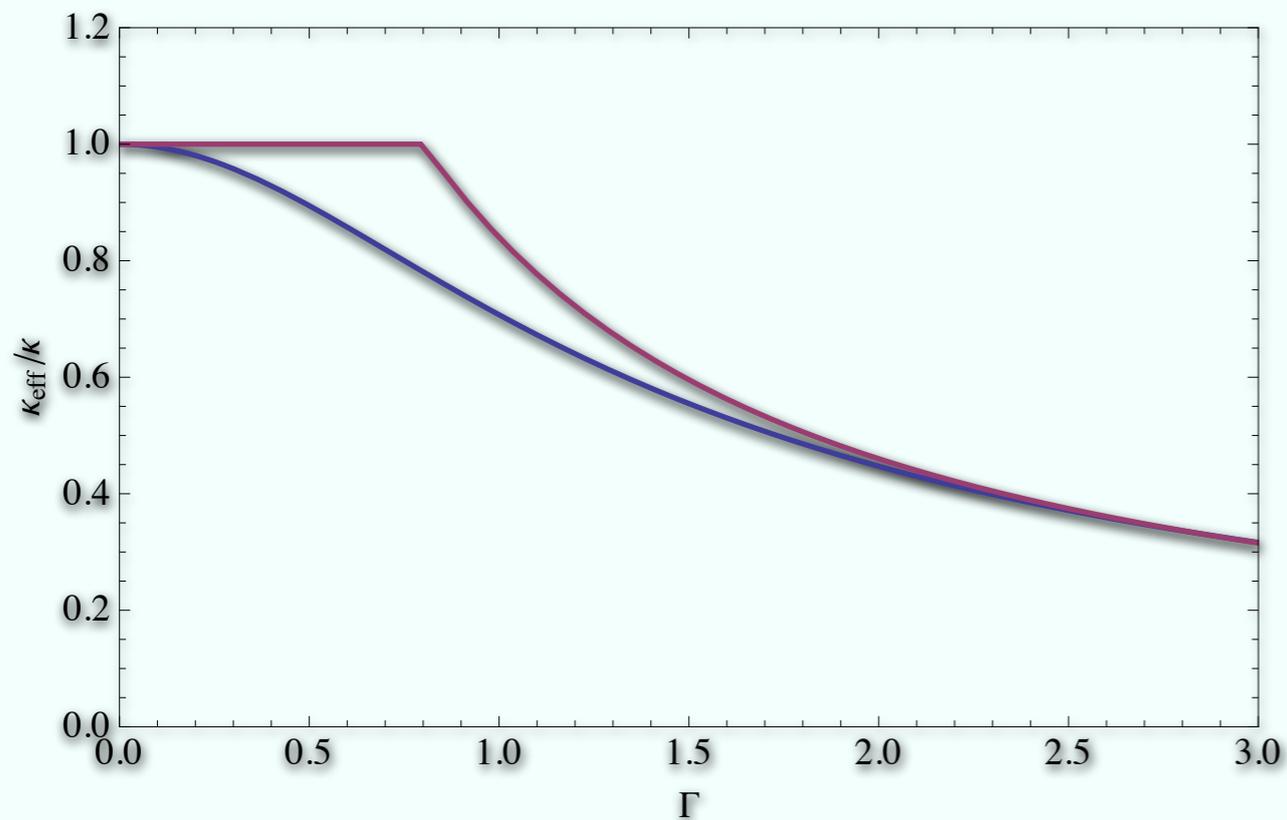
Reduction above  $\Gamma_{\text{crit}}$

$$\frac{\kappa_{\text{eff}}}{\kappa_0} = \left(1 - \frac{A}{\Gamma^B}\right) \frac{1}{\Gamma} \quad \text{for } \Gamma > \Gamma_{\text{crit}}$$

$$\frac{\kappa_{\text{eff}}}{\kappa_0} = 1 \quad \text{for } \Gamma < \Gamma_{\text{crit}}$$

Smooth Option:

$$\frac{\kappa_{\text{eff}}}{\kappa_0} = \frac{1}{(1 + \Gamma^p)^{1/p}}$$



# Super-Eddington Winds

- Local mass loss rate,

$$\dot{\Phi} = \mathcal{W} \frac{F - \mathcal{F}_{\text{Edd}}}{c v_s}$$

- Equation of motion,

$$\rho v_z \frac{dv_z}{dz} = - \frac{dP}{dz} - \rho g_z$$

- Energy conservation,

$$F(z) = F_{\text{atm}} - \dot{\Phi}_{\text{wind}} \left( \frac{v_z^2}{2} + \frac{GM_{\text{BH}}}{R_{\text{atm}}} - \frac{GM_{\text{BH}}}{R} \right)$$

# Photon Tired winds

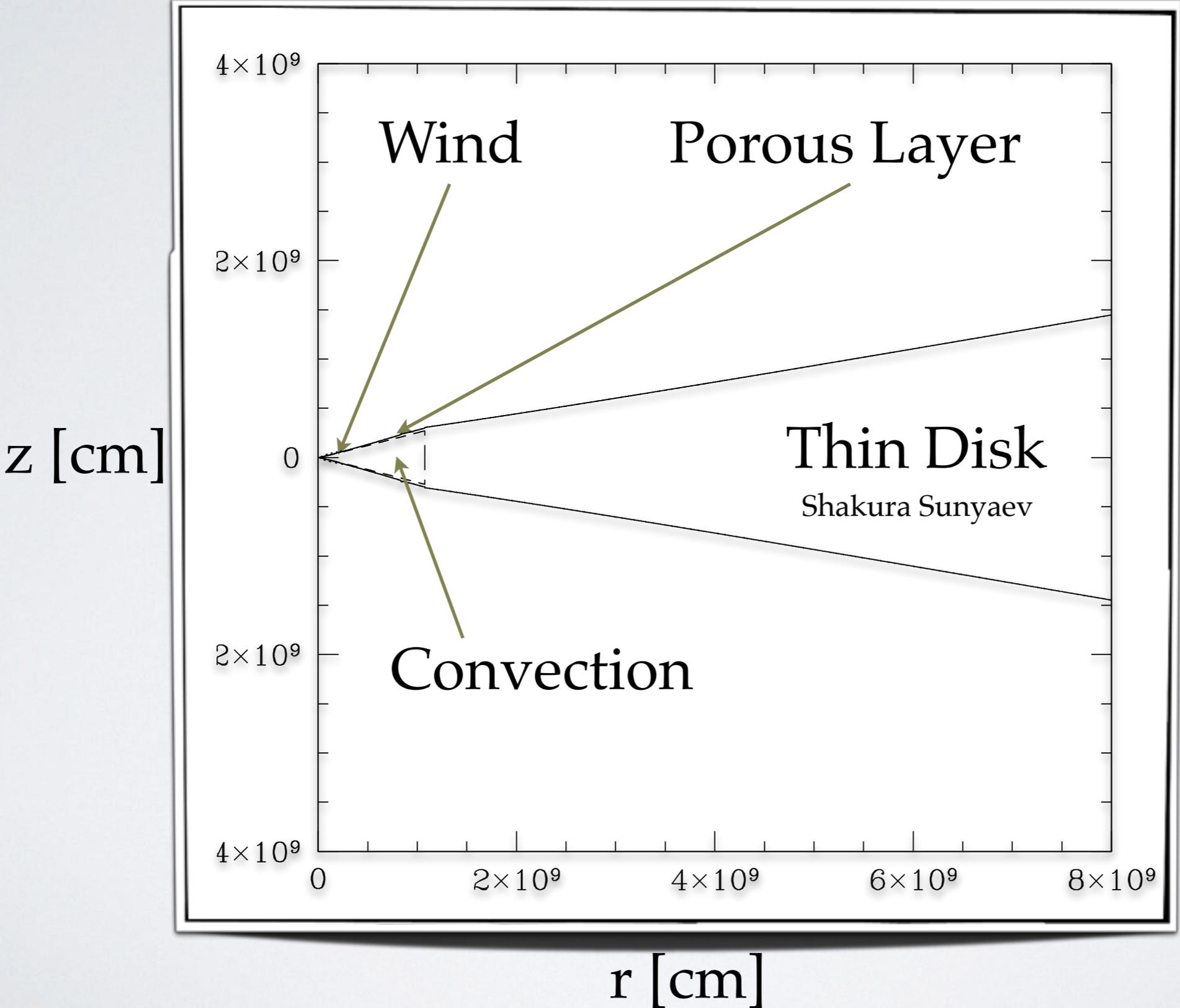
- When available radiative flux at the sonic point  $F_0$  is insufficient, photon tired wind is formed

$$\dot{\Phi}_{\text{tiring}} \equiv F / (GM_{\text{BH}} / R_{\text{atm}})$$

- Actual mass loss is reduced, (van Marle et al. 2009)

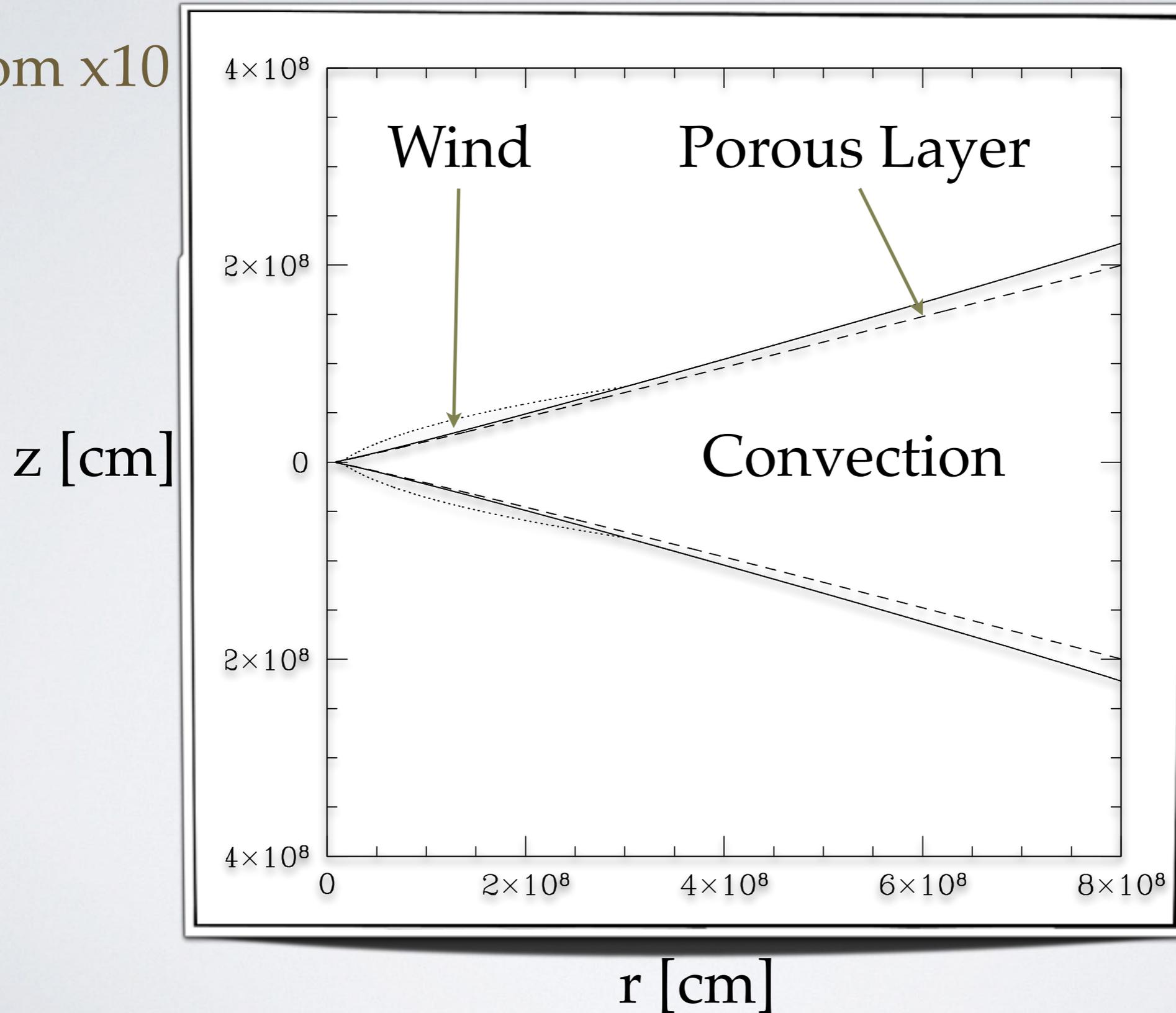
$$\frac{\dot{\Phi}_{\text{wind}}}{\dot{\Phi}_{\text{tiring}}} \simeq \max \left( 0.2 \left( \frac{F}{F_{\text{Edd}}} \right)^{0.6}, 0.9 \right)$$

# Real Appearance (1:1 Aspect ratio)



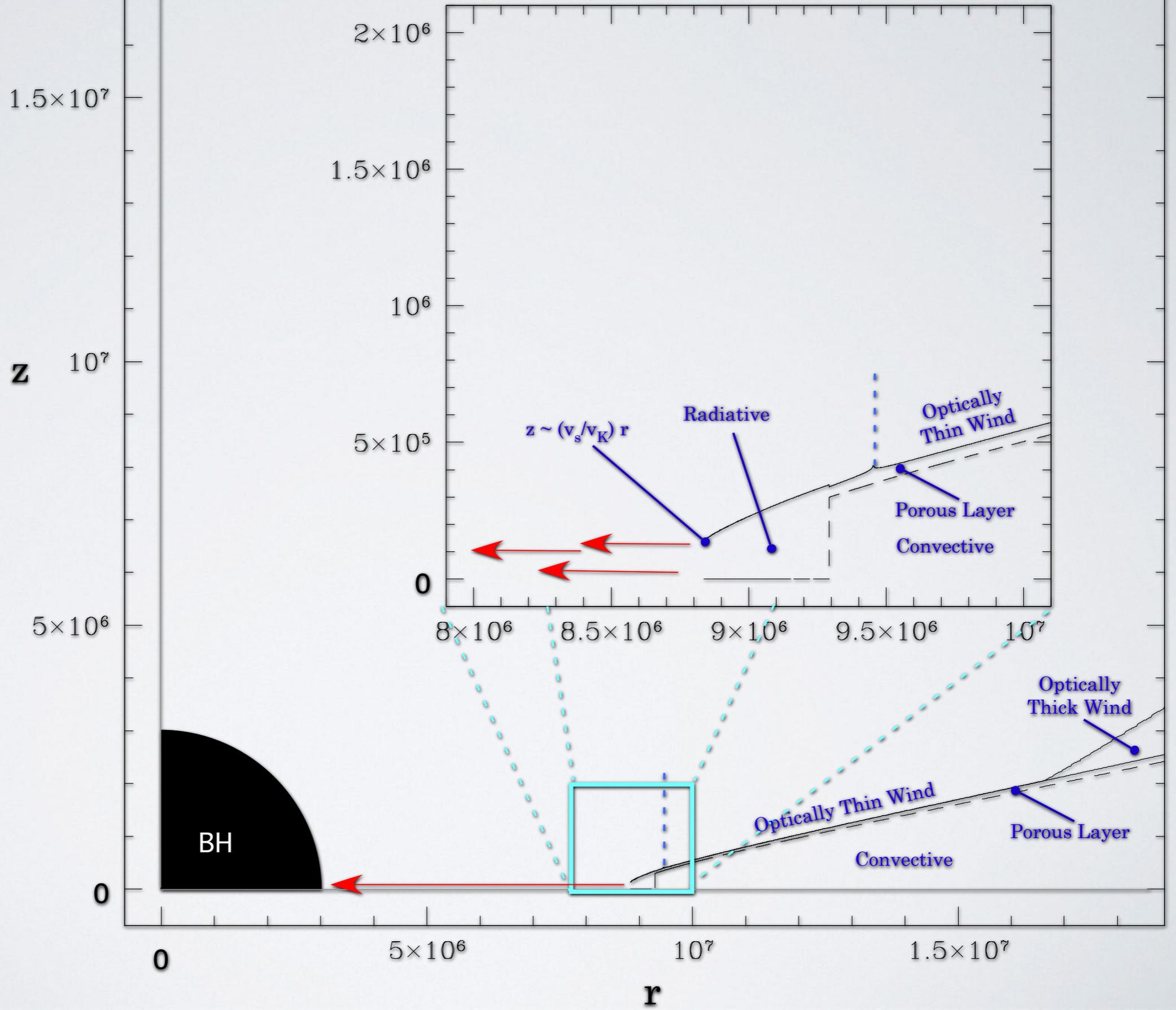
# Real Appearance (1:1 Aspect ratio), zoomed in

Zoom x10



# Near the ISCO

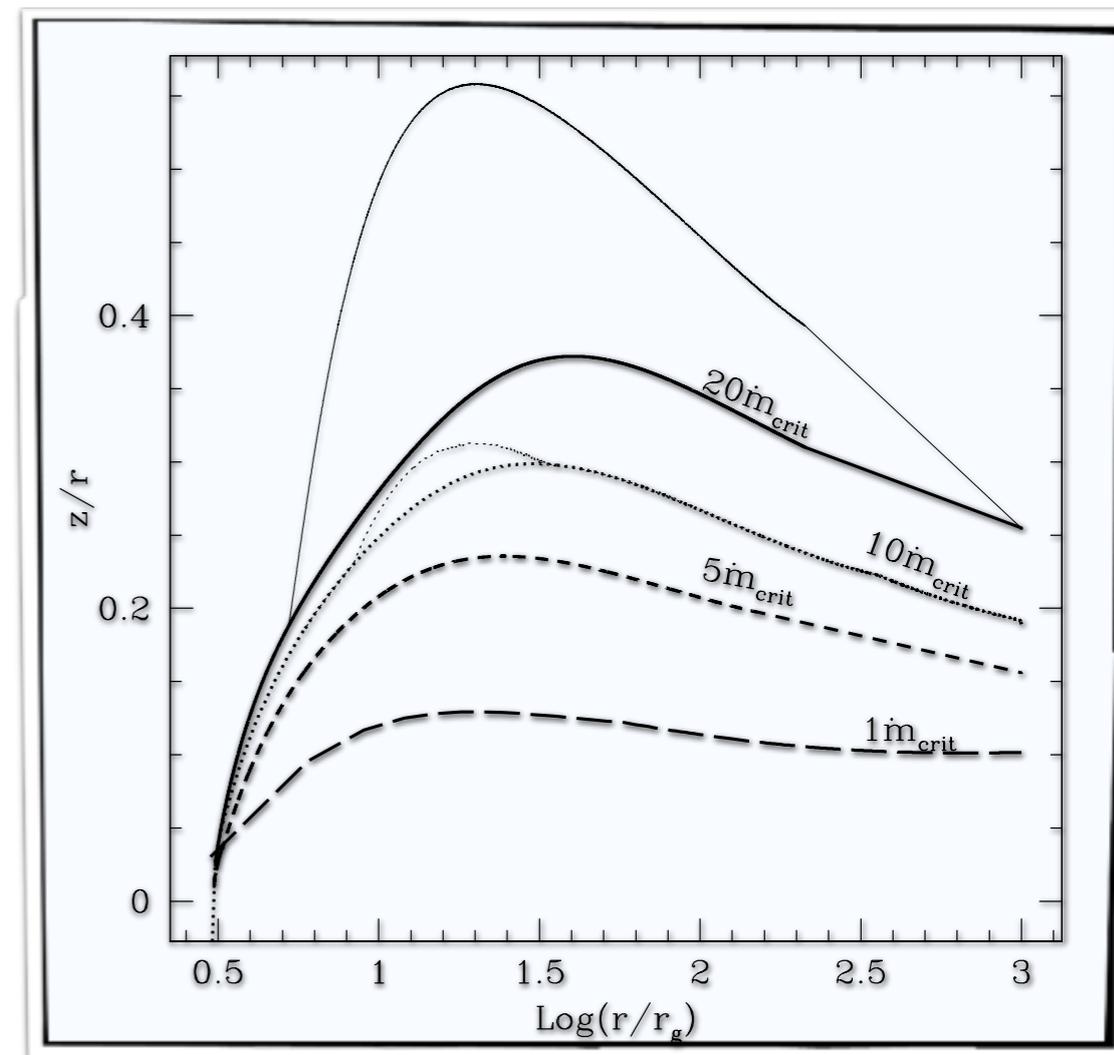
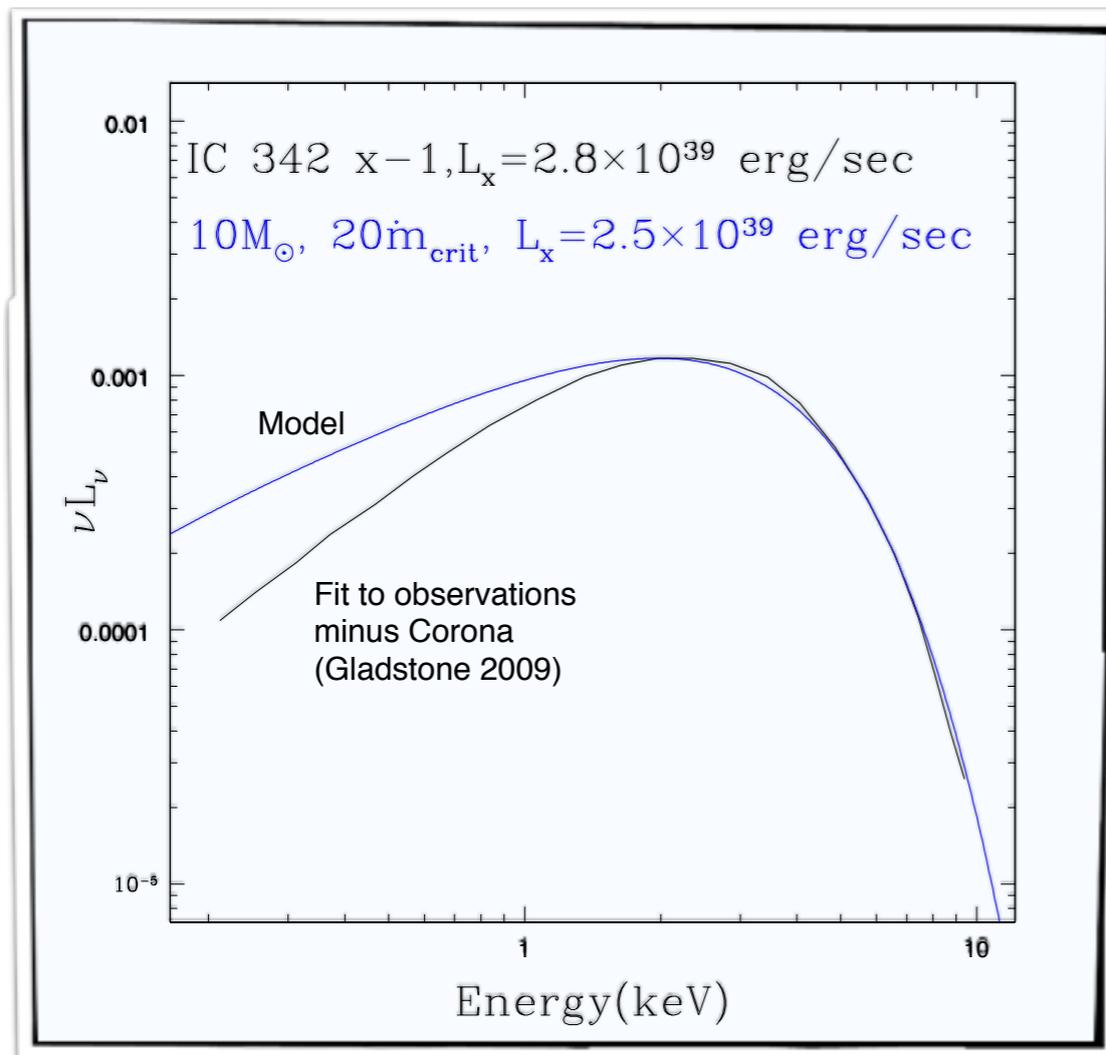
Zoom x400



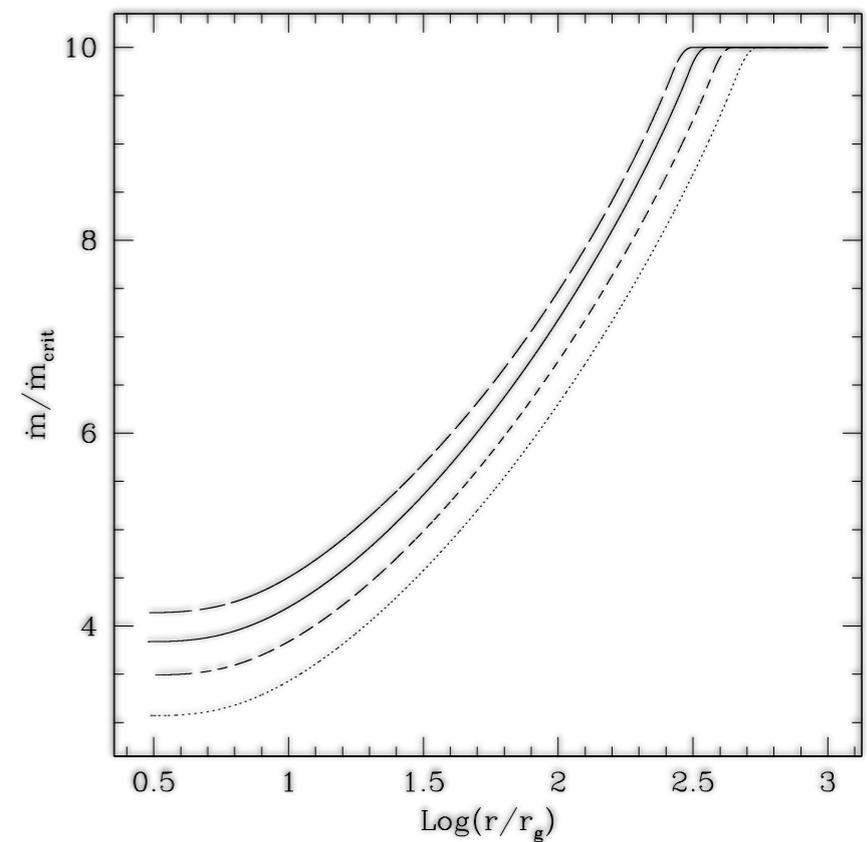
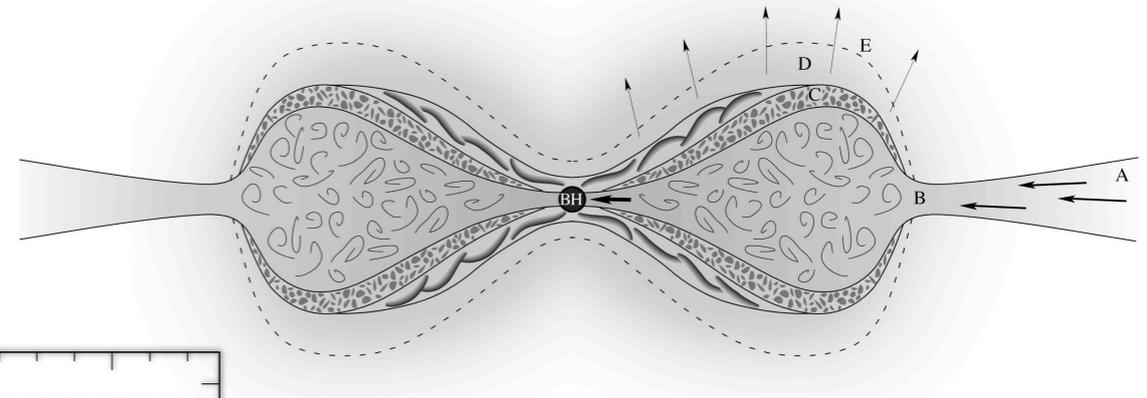
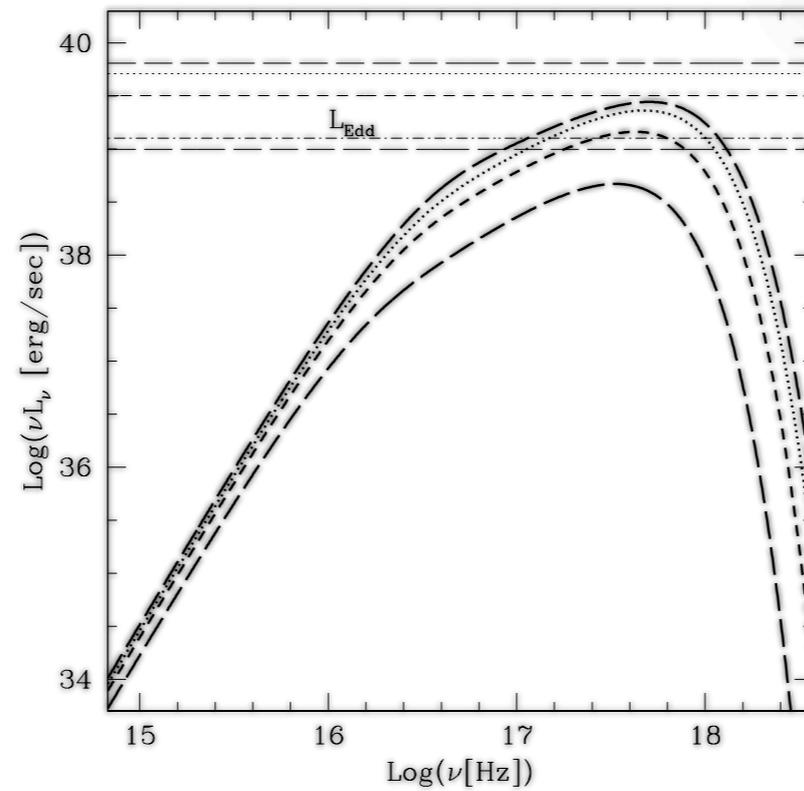
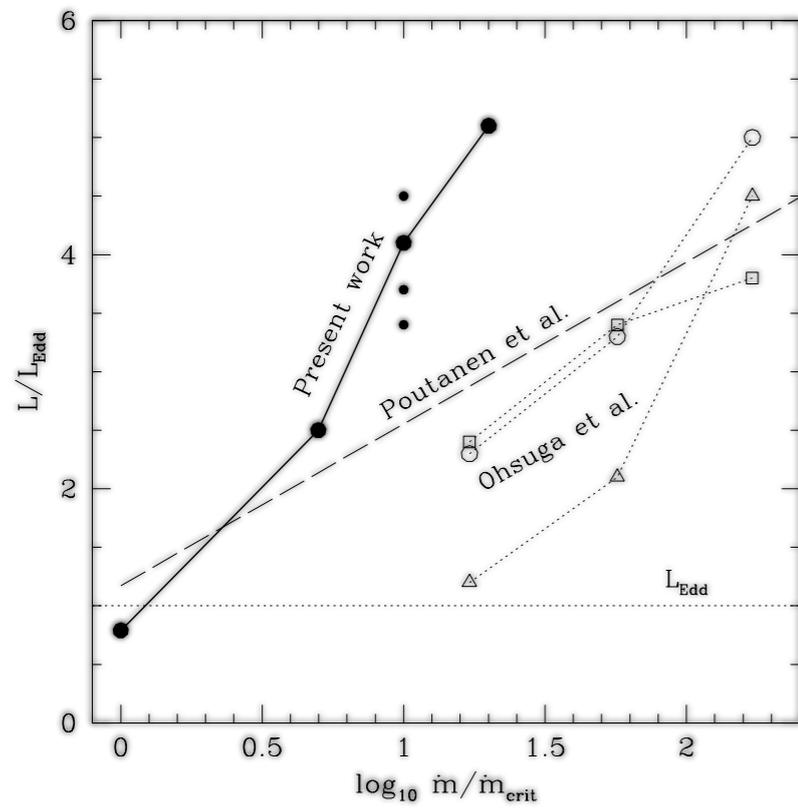
# Super-Eddington Slim Accretion

Dotan & Shaviv 2012

- Super-Edd states allow for super-Eddington accretion
- Predicted X-ray spectrum consistent with observations

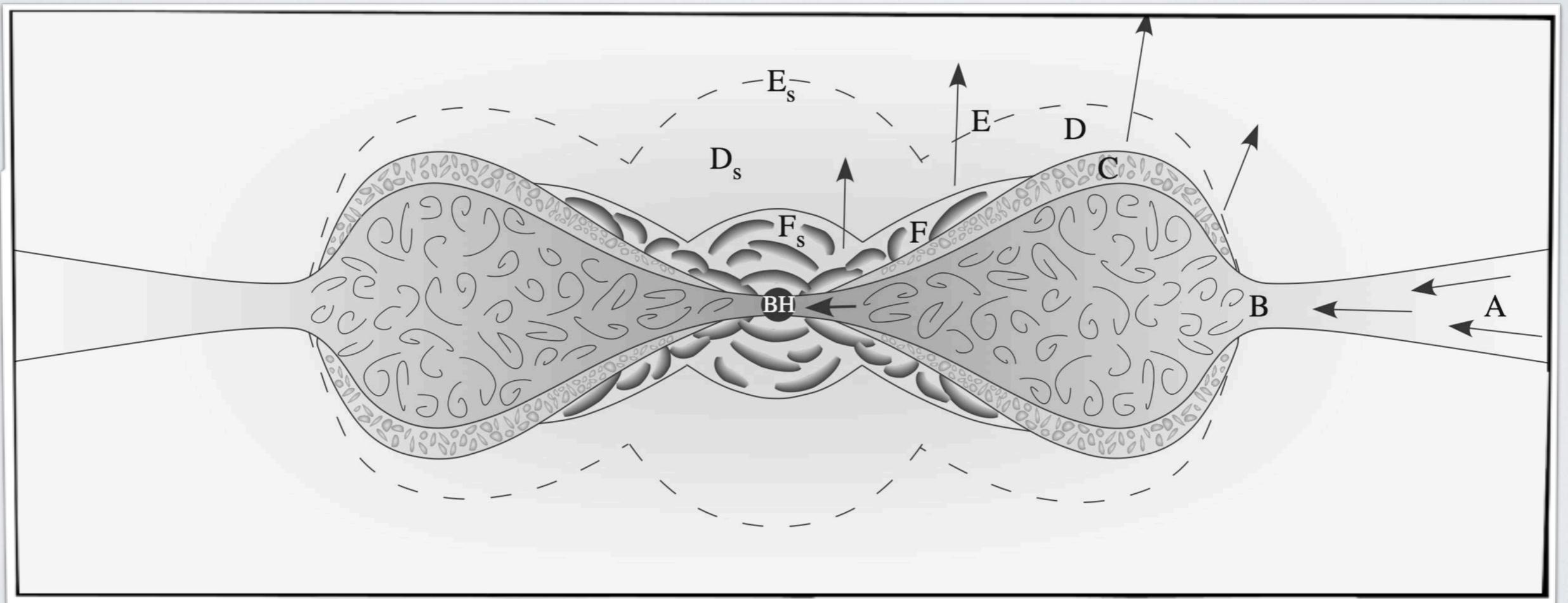


# Predicts super-Eddington Accretion



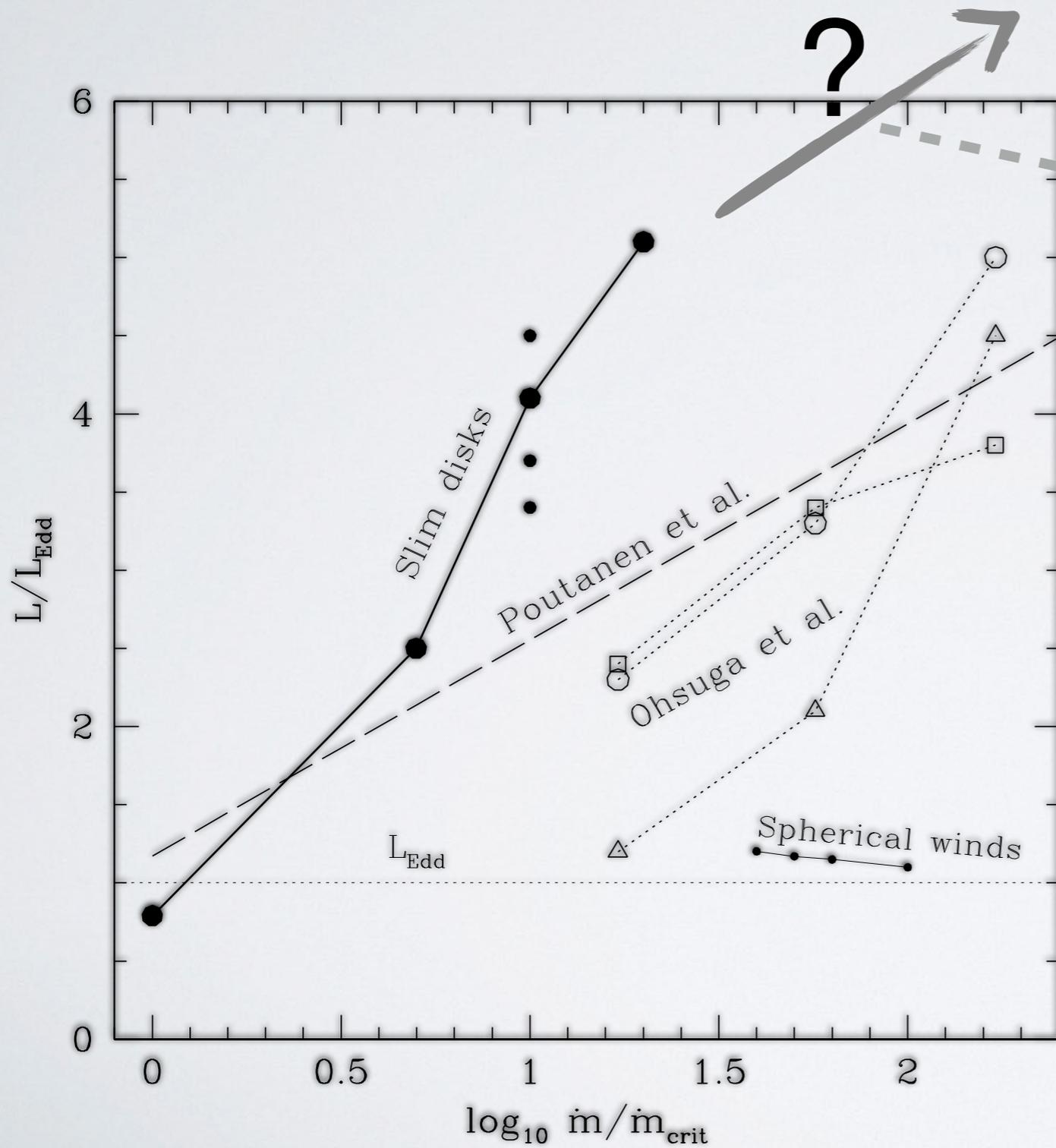
# For high accretion rates

- For  $\dot{M} > 30 \dot{M}_{\text{crit}}$ ,  $z_{\text{ph}} > r \rightarrow$  inconsistent solution
- Wind becomes spherical?



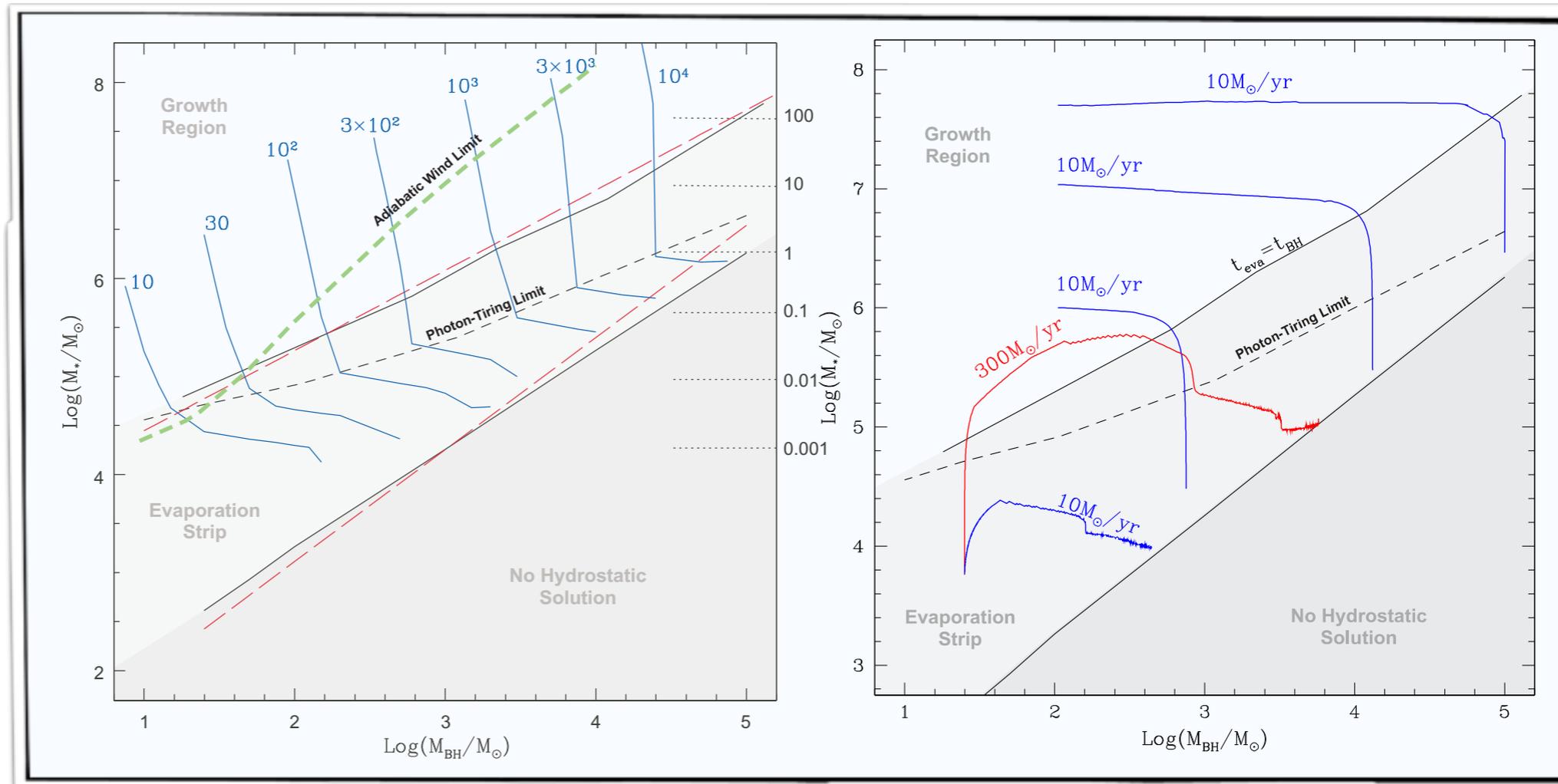
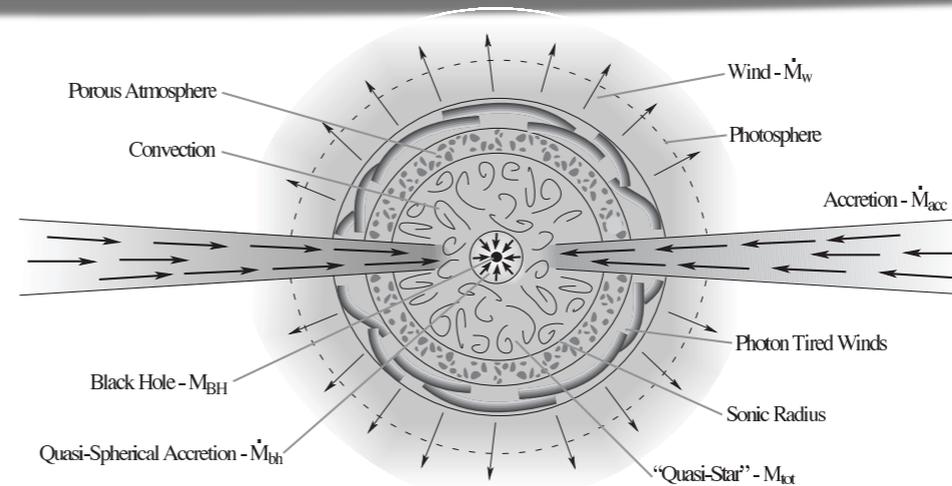
Slim disks with spherical winds

# For high accretion rates



# Quasi-star accretion

- Another accretion geometry is that of "quasi-stars"



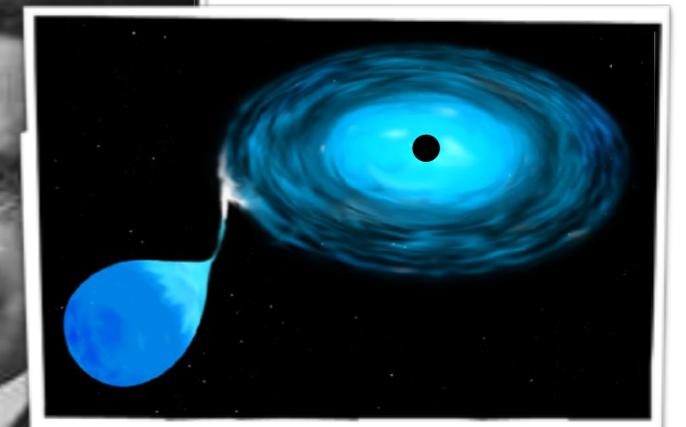
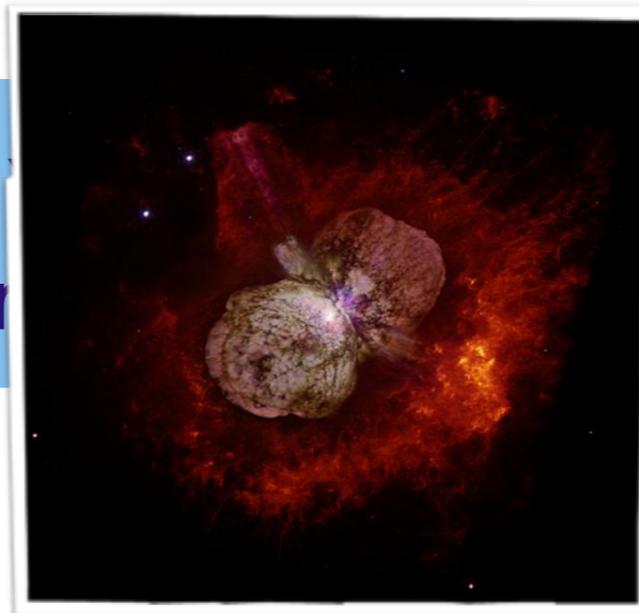
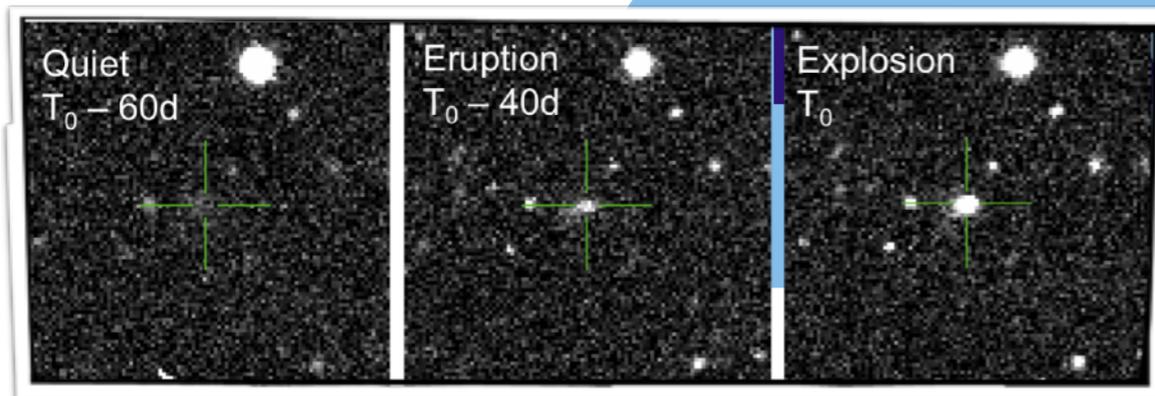
# Summary

- The Eddington luminosity is not a limit!

- Super-Eddington states exist  
They have strong winds

$$\dot{m} = \mathcal{W} \frac{(L - L_{Edd})}{v_s c}$$

- Super-Eddington states explain a range of astrophysical phenomena



# Thanks

- Stan Owocki, Shlomi Pistinner (Winds)
- Irit Idan, Giora Shaviv (Stars)
- Calanit Dotan & Elena Rossi (Accretion)
- Yair Arcavi & Avishai Gal Yam (In precursors, SN imposters)